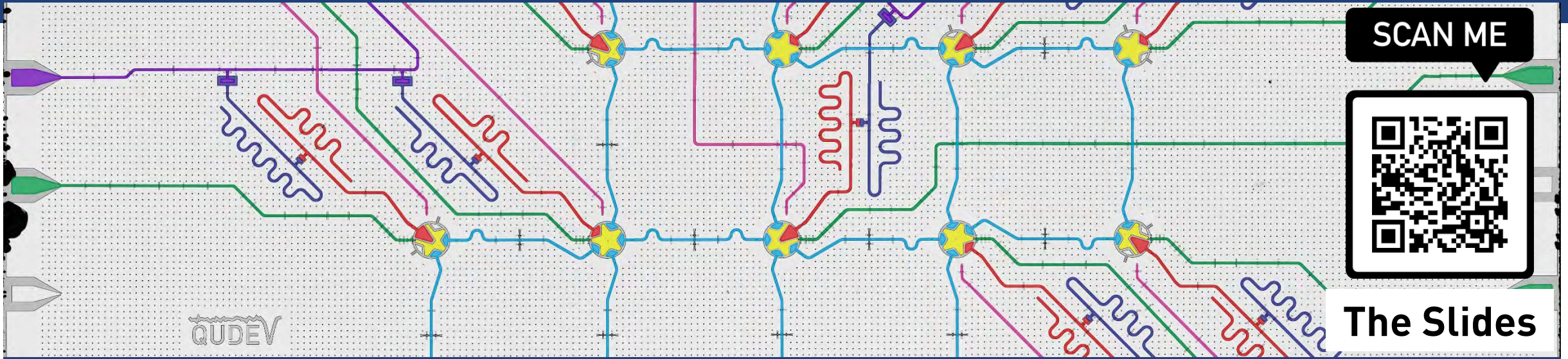


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SCAN ME



The Slides



# Quantum Error Correction for Superconducting Quantum Information Processors

Sci. Team: E. Al-Tavil, L. Beltran, I. Besedin, J.-C. Besse, D. Colao Zanuz, Xi Dai, K. Dalton, J. Ekert, S. Frasca, A. Grigorev, D. Hagmann, C. Hellings, A. Hernandez-Anton, I. Hesner, L. Hofele, M. Kerschbaum, J. Knoll, A. Kulikov, N. Lacroix, M. Pechal, K. Reuer, A. Rosario, C. Scarato, J. Schaer, Y. Song, F. Swiadek, J. Trebst, F. Wagner, A. Wallraff *(ETH Zurich)*

L. Bödeker, L. Colmenarez, M. Müller *(RWTH Aachen)*

Eng. & Tech. Team: M. Bahrani, A. Flasby *(ETH Zurich)*



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Schweizerischer  
Nationalfonds

Innovation project  
supported by



Schweizerische Eidgenossenschaft  
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Swiss Confederation

Innosuisse – Swiss Innovation Agency

# The Quantum Device Lab



Innovation project  
supported by

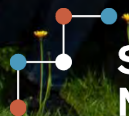


Schweizerische Eidgenossenschaft  
Confédération suisse  
Confederazione Svizzera  
Confederaziun svizra  
Swiss Confederation  
Innosuisse – Swiss Innovation Agency



IA RPA  
BE THE FUTURE

with fall-term project students



# Past Group Members & Current Collaboration Partners

[www.qudev.ethz.ch](http://www.qudev.ethz.ch)

## Former group members now Faculty/PostDoc/PhD/Industry

A. Abdumalikov (Gorba AG)  
M. Allan (LMU Munich)  
C. K. Andersen (TU Delft)  
M. Baur (ABB)  
J. Basset (U. Paris Sud)  
S. Berger (AWK Group)  
R. Bianchetti (ABB)  
D. Bozyigit (Scandit)  
R. D. Buijs (ASML)  
M. Collodo (Zurich Instruments)  
A. Copetudo (NU Singapore)  
C. Eichler (FAU Erlangen)  
A. Fedorov (UQ Brisbane)  
Q. Ficheux (CNRS Grenoble)  
S. Filipp (WMI & TU Munich)  
J. Fink (IST Austria)  
A. Fragner (Kappa)  
T. Frey (Bosch)  
M. Gabureac (PSI)  
S. Garcia (College de France)  
S. Gasparinetti (Chalmers)  
M. Goppl (Sensirion)  
J. Govenius (VTT)

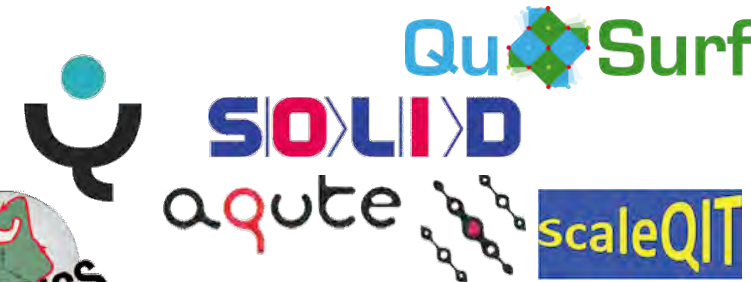
J. Heinsoo (IQM)  
J. Herrmann (QuantrolOx)  
L. Huthmacher (Stellbrink & Prtnr)  
D.-D. Jarausch (Leica)  
K. Juliusson (IQM)  
P. Kurpiers (Rohde & Schwarz)  
J. Krause (U. Of Cologne)  
S. Krinner (Zurich Instruments)  
N. Lacroix (Google)  
C. Lang (Radionor)  
S. Lazar (Zurich Instruments)  
P. Leek (Oxford)  
S. M. Llima (BSC-CNS)  
J. Luetolf (D-PHYS, ETH Zurich)  
P. Magnard (Alice and Bob)  
P. Maurer (Chicago)  
J. Mlynek (Siemens)  
M. Mondal (IACS Kolkata)  
G. Norris (AWS)  
M. Oppliger  
J. O'Sullivan (CEA Saclay)  
A. Potocnik (imec)  
G. Puebla (QZabre)  
A. Remm (Atlantic Quantum)  
K. Reuer (d-fine)

A. Safavi-Naeini (Stanford)  
Y. Salathe (Zurich Instruments)  
P. Scarlino (EPF Lausanne)  
M. Stammeier (Huba Control)  
L. Steffen (AWK Group)  
A. Stockklauser (Rigetti)  
T. Thiele (Zurich Instruments)  
I. Tsitsilin (TUM)  
J. Ungerer (Harvard)  
A. van Loo (RIKEN)  
D. van Woerkom (Microsoft)  
J. Waissman (HUJI)  
T. Walter (deceased)  
L. Wernli (Sensirion)  
A. Wulff  
S. Zeytinoğlu (Harvard)

I. Cirac (MPQ)  
K. Ensslin (ETH Zurich)  
M. Hartmann (FAU Erlangen)  
T. Ihn (ETH Zurich)  
A. Imamoglu (ETH Zurich)  
F. Marquardt (MPL Erlangen)  
F. Merkt (ETH Zurich)  
A. Messmer (Zurich Instruments)  
M. W. Mitchell (ICFO)  
M. Müller (RWTH Aachen, FZJ)  
M. A. Martin-Delgado (Madrid)  
M. Poggio (Basel)  
B. Royer (Sherbrooke)  
N. Sangouard (CEA Saclay)  
H. Tureci (Princeton)  
W. Wegscheider (ETH Zurich)

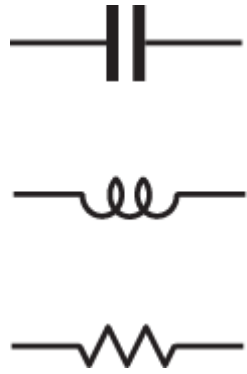
## Collaborations (last 5 years) with groups of

C. Abellan (Quside)  
P. Bertet (CEA Saclay)  
A. Blais (Sherbrooke)  
J. Bylander (Chalmers)  
H. J. Carmichael (Auckland)  
A. Chin (Cambridge)

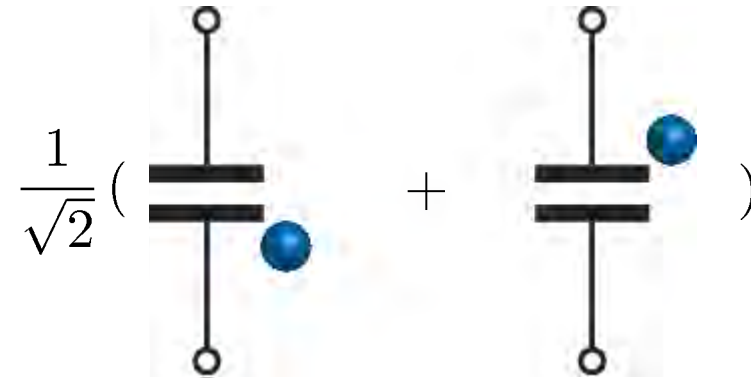


# Quantum Physics with Electronic Circuits

basic circuit elements:



charge on a capacitor:



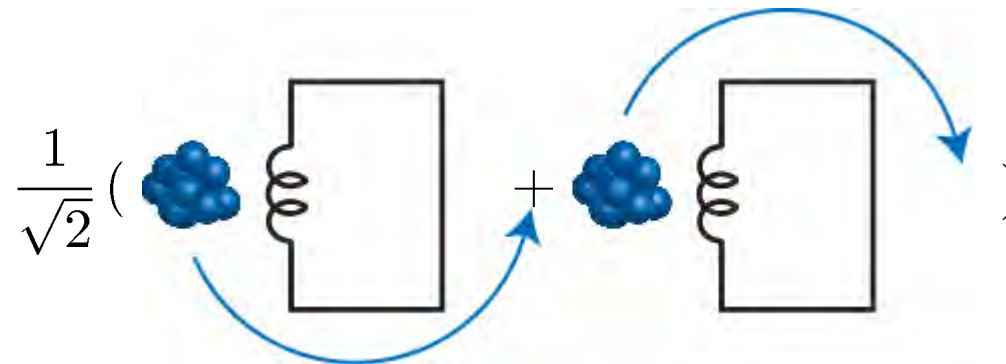
quantum superposition states of:

- charge  $Q$
- flux  $\phi$

$Q, \phi$  are conjugate variables

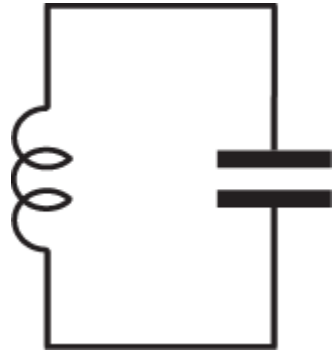
commutation relation  $[\hat{\phi}, \hat{Q}] = i\hbar$

current or magnetic flux in an inductor:



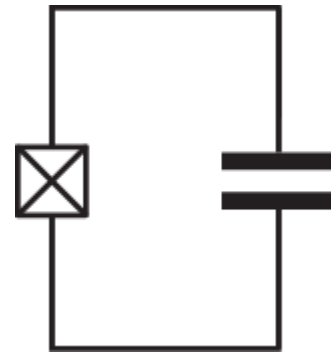
# Linear and Nonlinear Superconducting Electronic Oscillators

LC resonator:

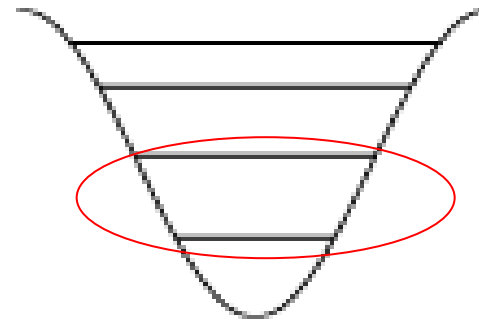
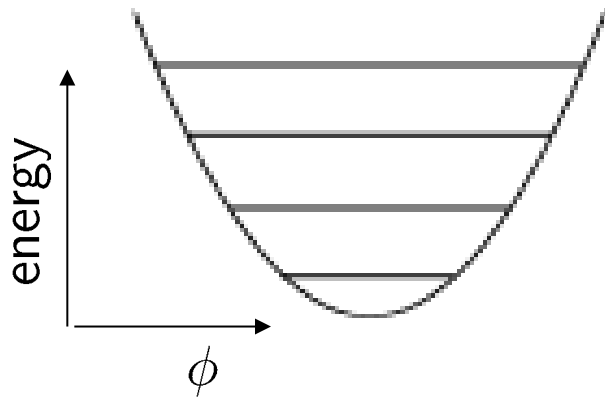


Josephson junction resonator:

Josephson junction = nonlinear inductor



anharmonicity defines effective two-level system



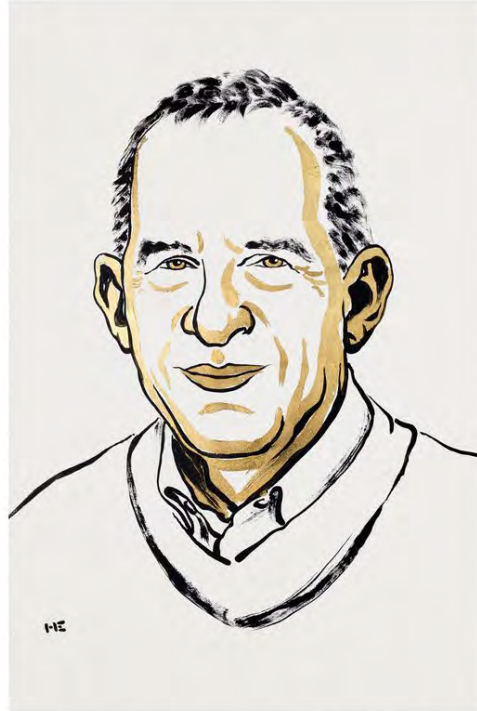
# Nobel Prize in Physics 2025: Macroscopic Quantum Tunneling and Energy Level Quantization in Electrical Circuits



Ill. Niklas Elmehed © Nobel Prize Outreach

**John Clarke**

Prize share: 1/3



Ill. Niklas Elmehed © Nobel Prize Outreach

**Michel H. Devoret**

Prize share: 1/3



Ill. Niklas Elmehed © Nobel Prize Outreach

**John M. Martinis**

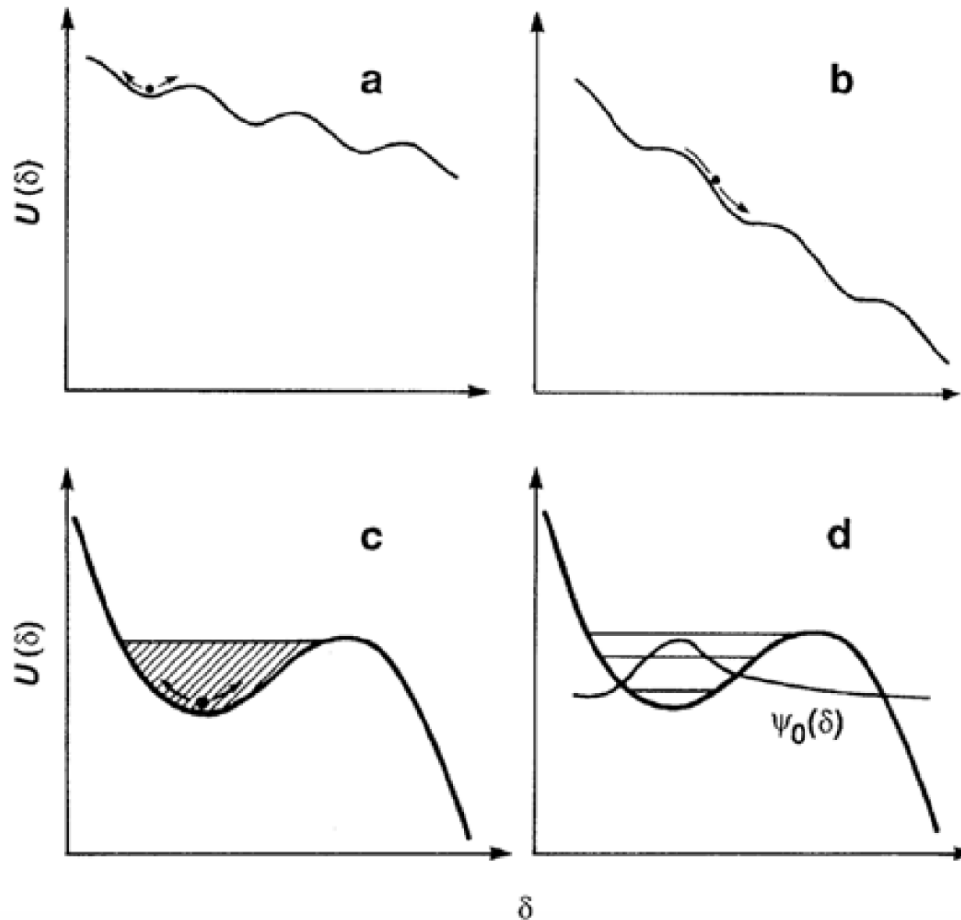
Prize share: 1/3

Physics 2025



The Nobel Prize in Physics 2025 was awarded jointly to John Clarke, Michel H. Devoret and John M. Martinis "for the discovery of macroscopic quantum mechanical tunnelling and energy quantisation in an electric circuit"

# Thermal Activation and Quantum Tunneling in a Current-Biased Josephson Junction



Tilted washboard potential

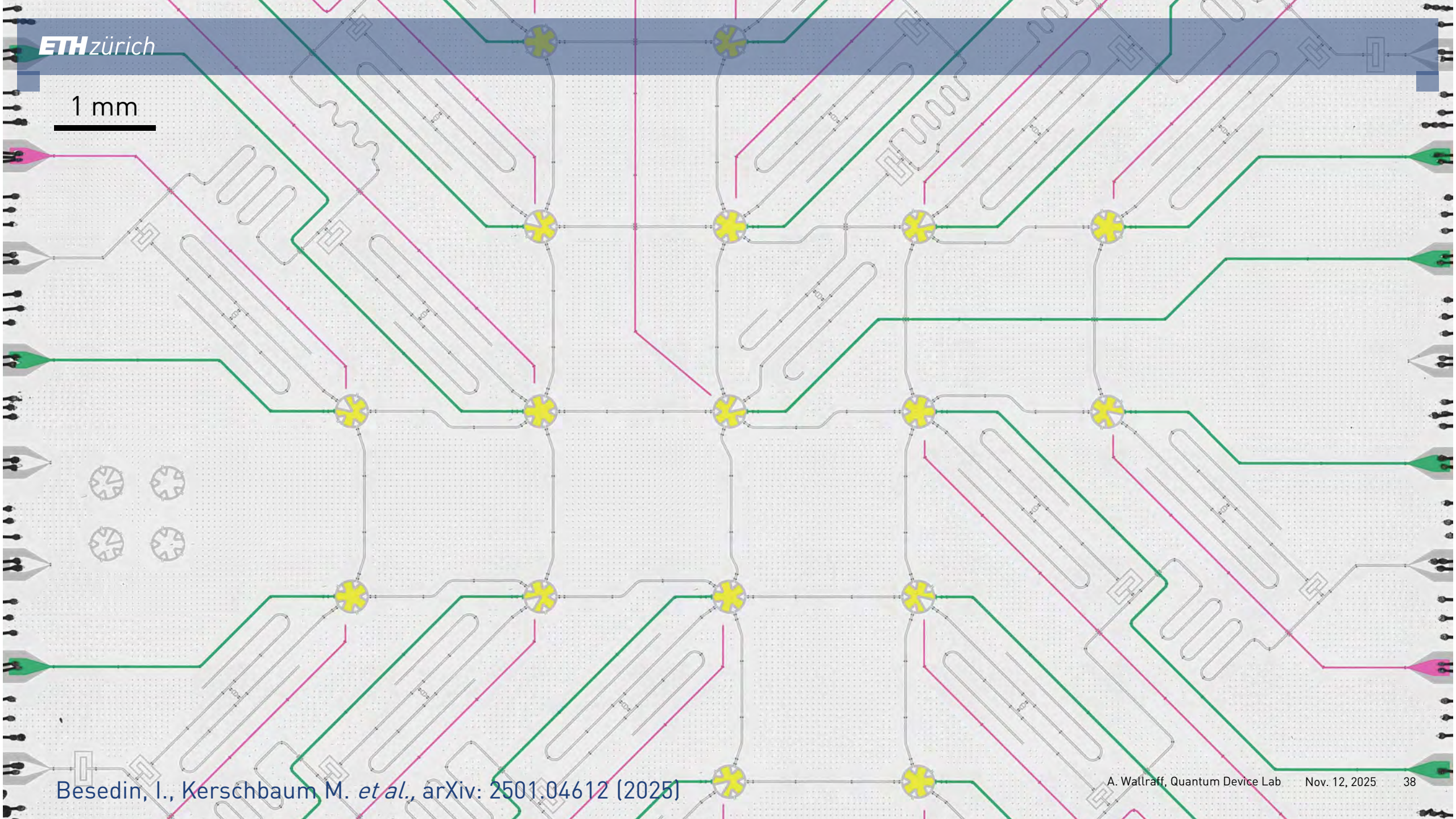
1 mm

**17 Qubits, with 24 Coplanar Waveguide Resonators for Two-Qubit Coupling  
and 17 Resonator-Purcell-Filter Pairs for Qubit Readout.**

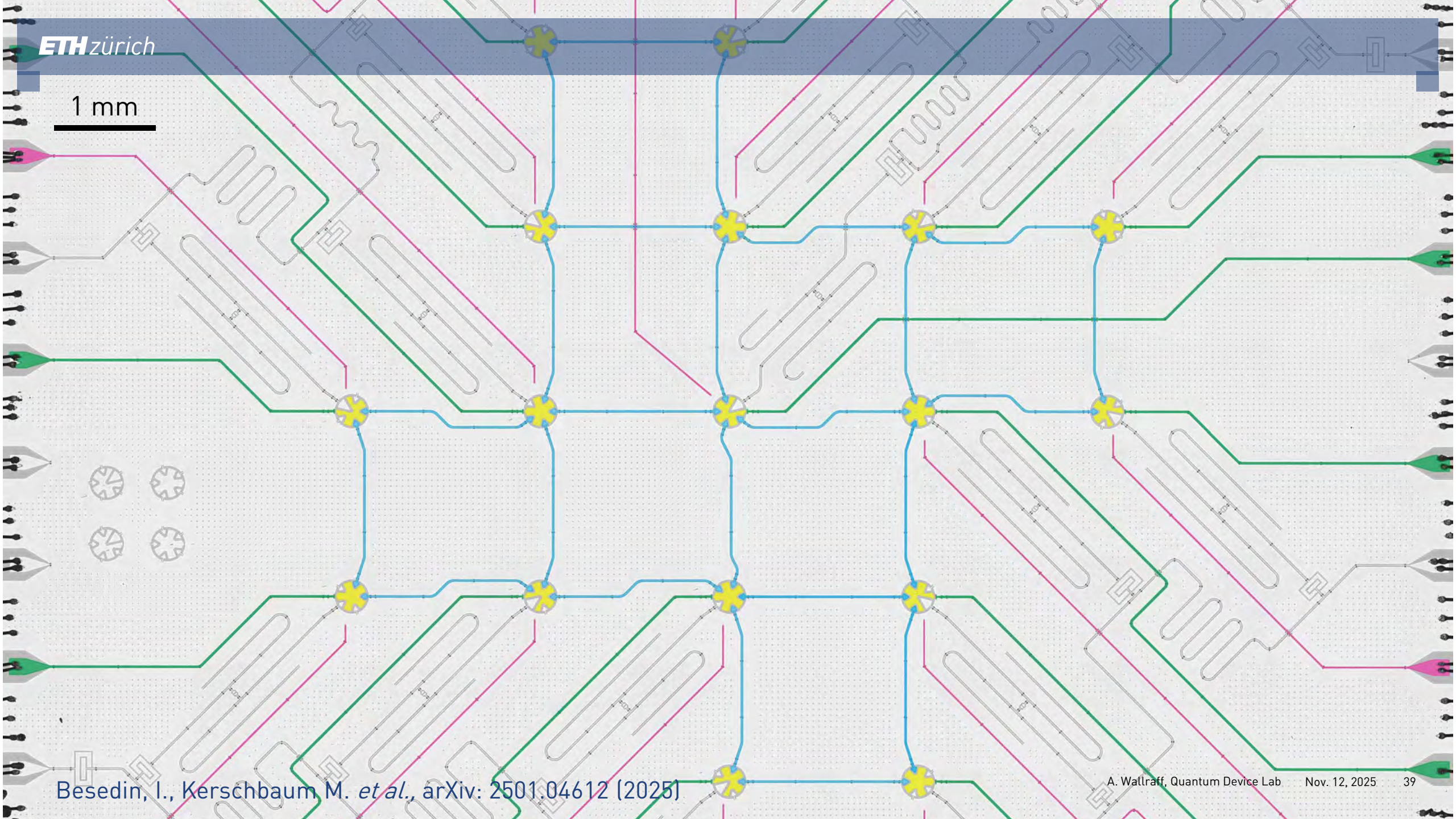
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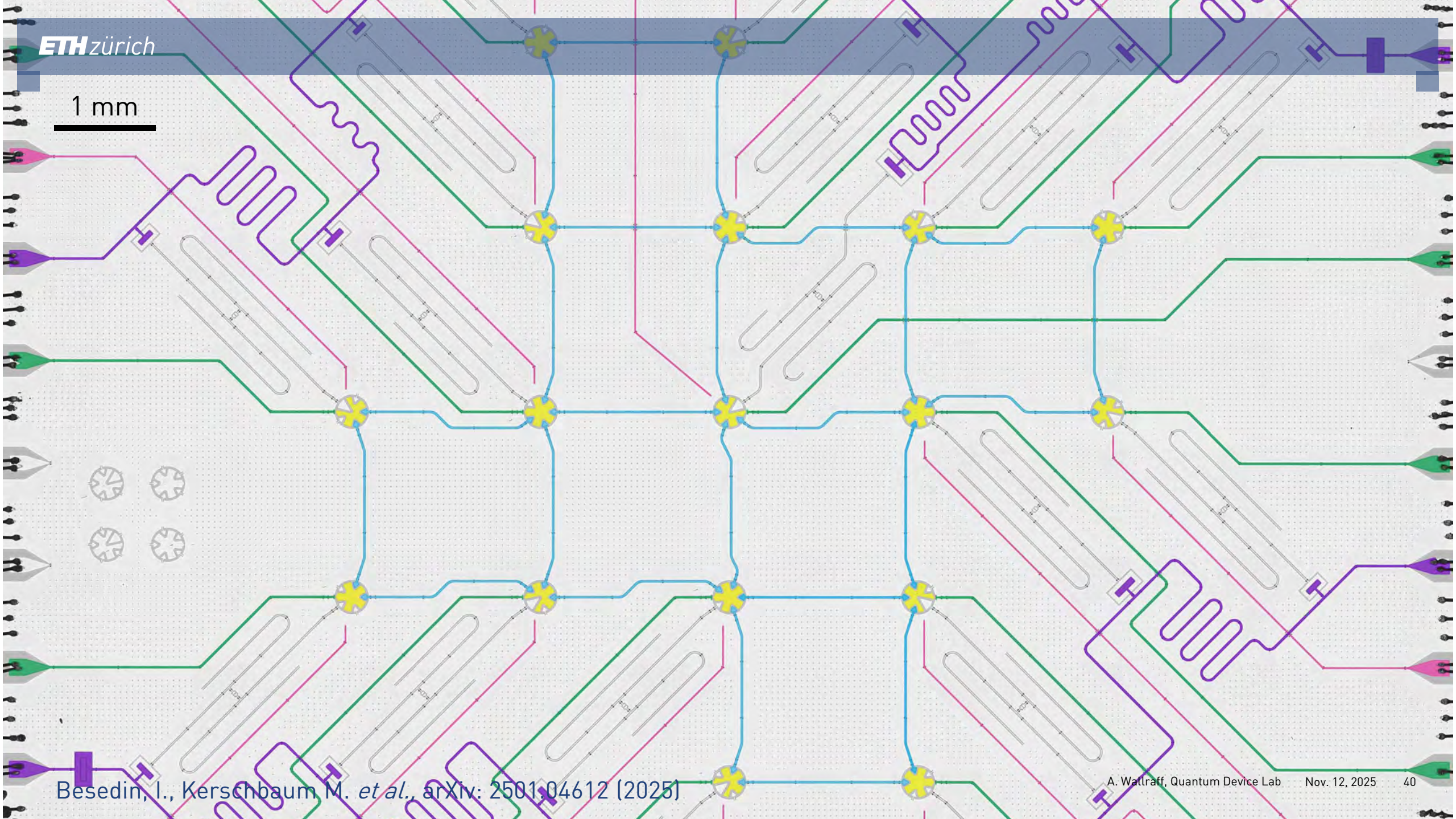
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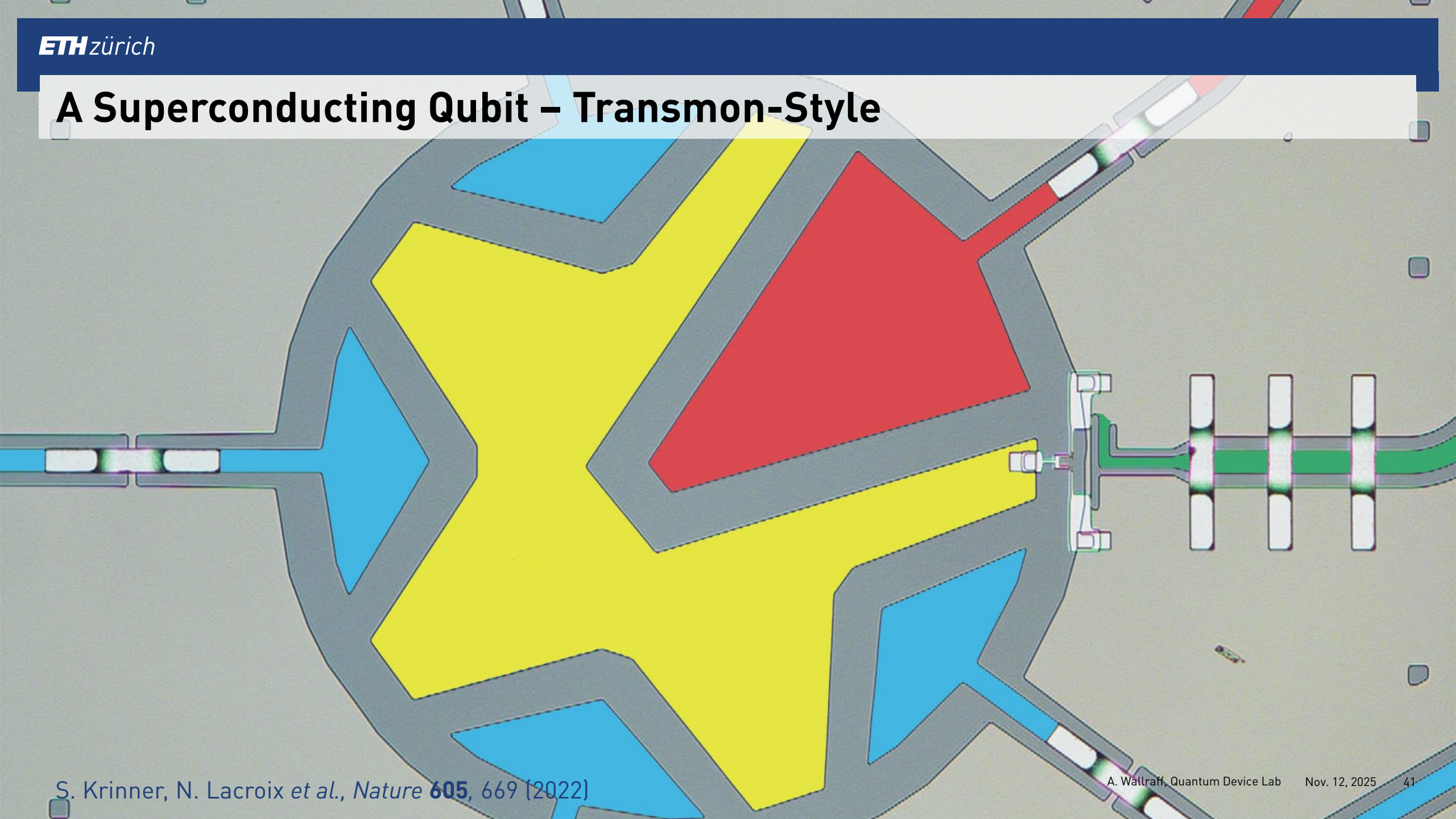
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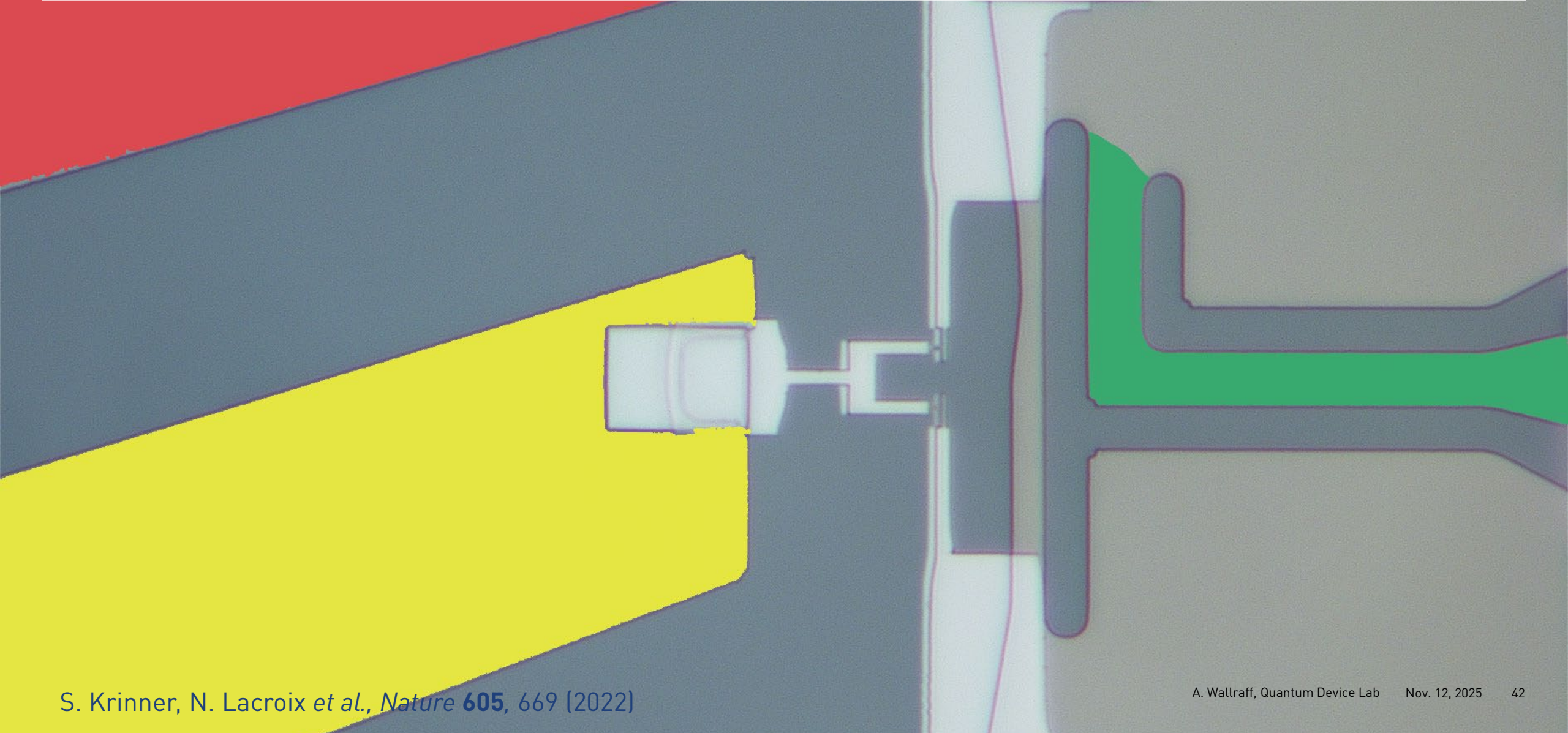
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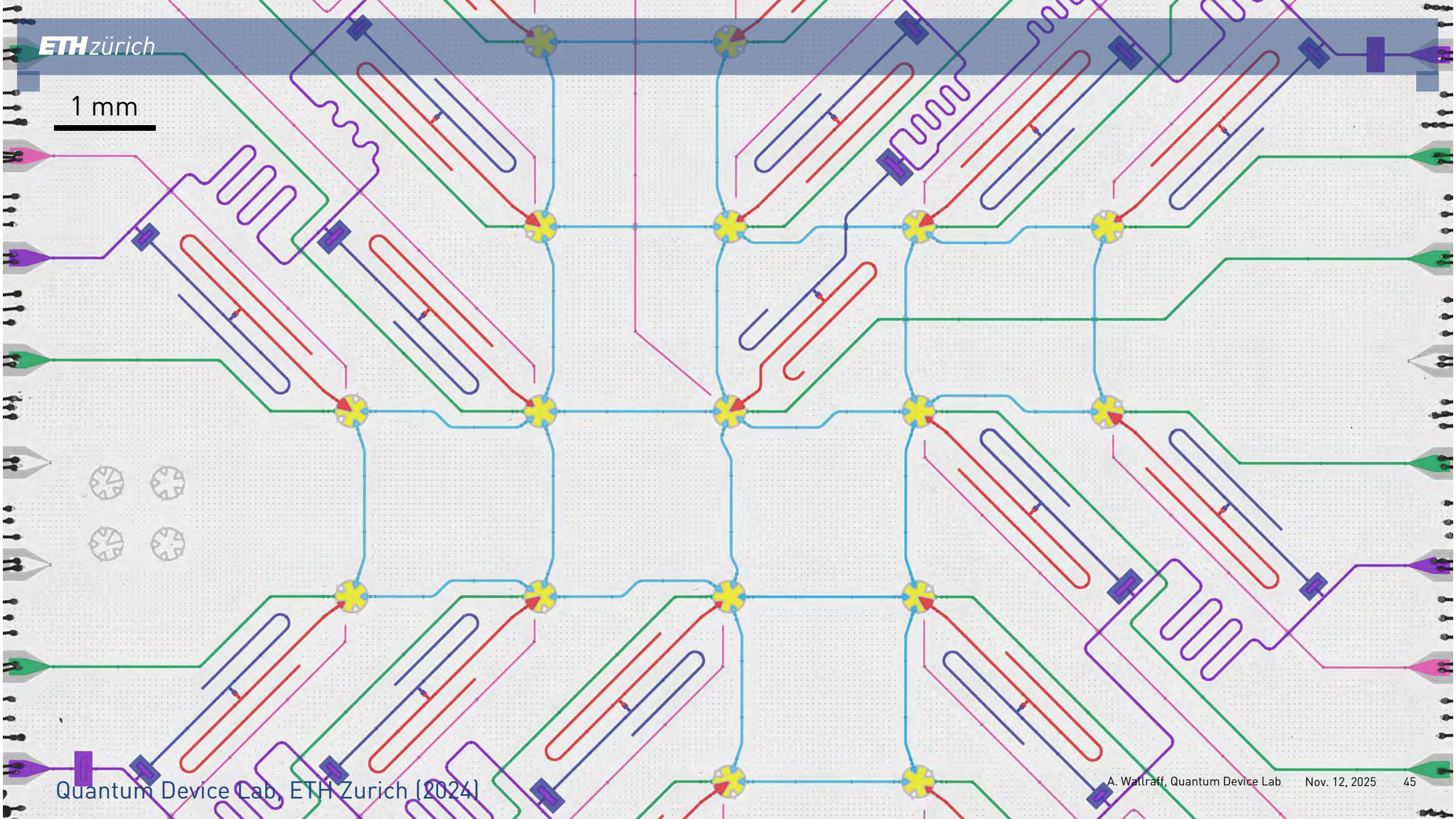
# A Superconducting Qubit – Transmon-Style



# Tunnel Junctions, SQUID, and Fluxline



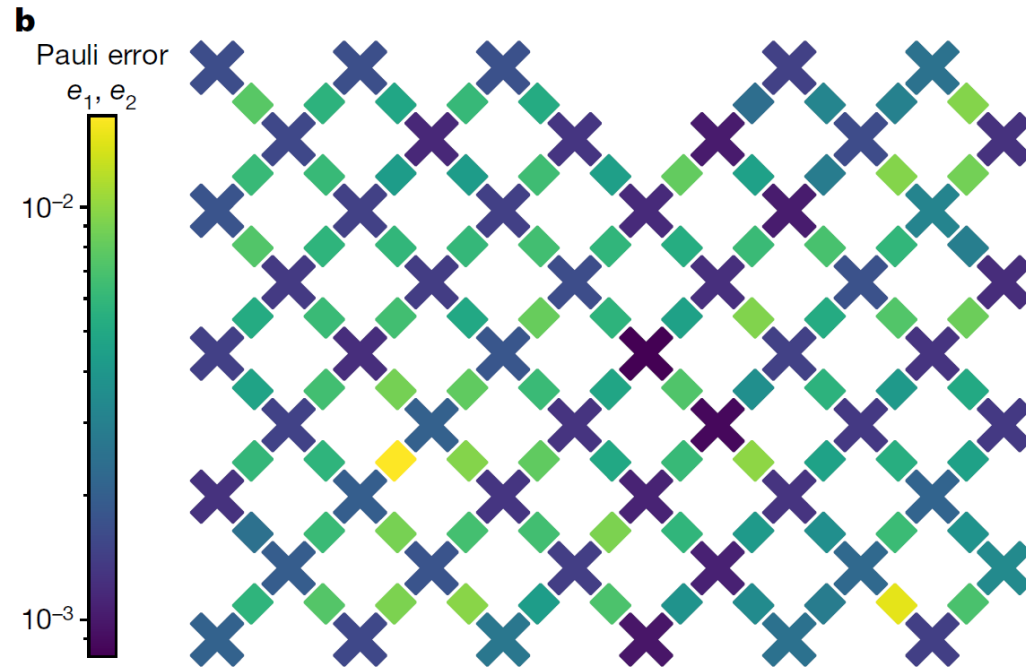
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# Two of the Major Goals in Quantum Information Processing ...

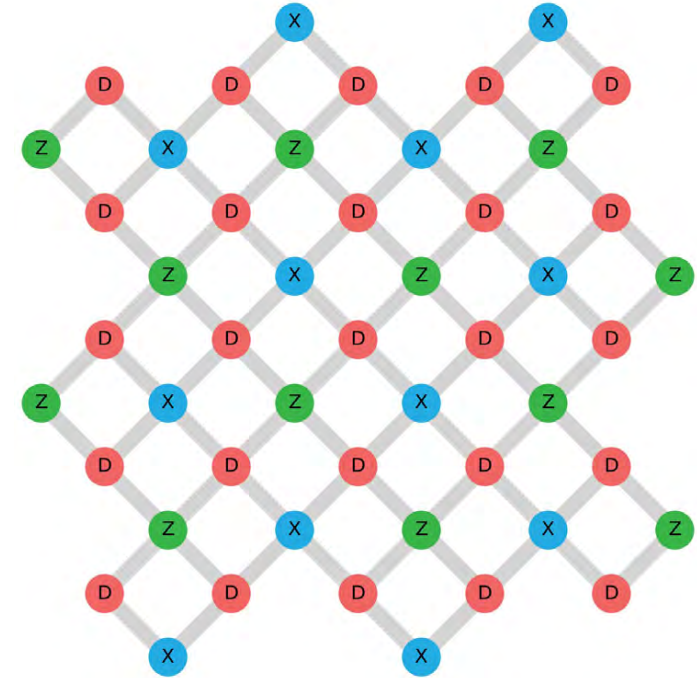
... with superconducting circuits

Noisy Intermediate Scale Quantum (NISQ) algorithms displaying a quantum advantage



F. Arute, ..., J. M. Martinis *et al.*, *Nature* **574**, 505 (2019)

Fault-tolerant, error-corrected, universal quantum information processor



Fowler *et al.*, *Phys. Rev. A* **86**, 032324 (2012)

# The Challenge of Quantum Error Correction

Detect and correct two types of errors:

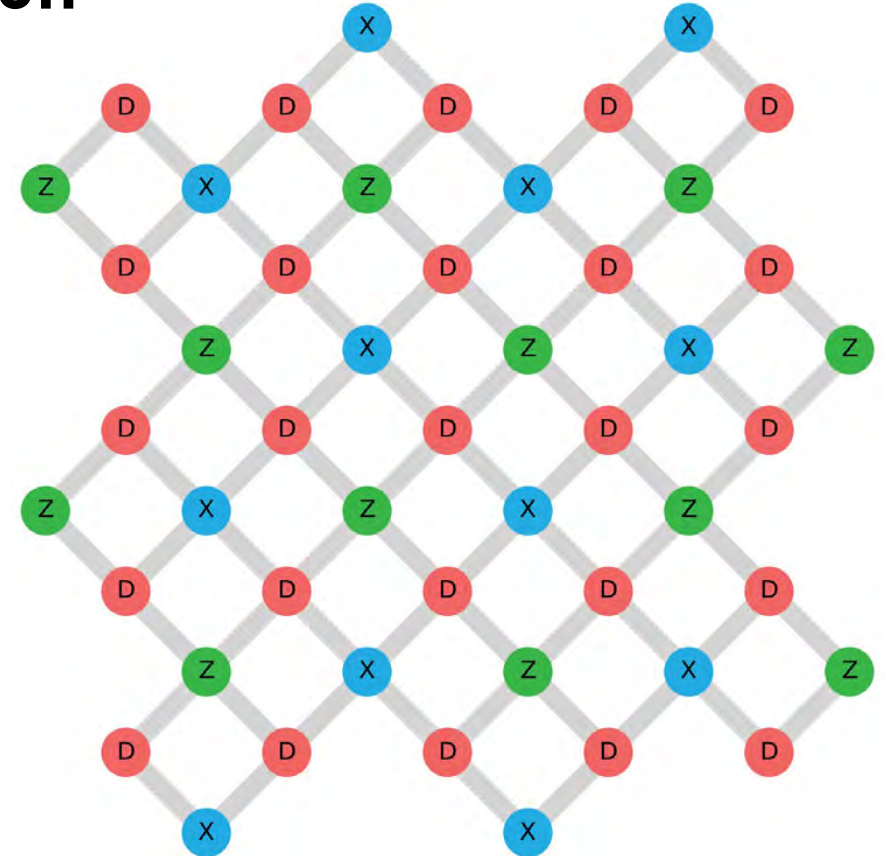
- Bit flips
- Phase flips

Preserve stored quantum states while detecting and correcting errors:

- Measurements collapse quantum (superposition) states

Solution: Use encoding

- Store **logical qubit** state  $|\psi\rangle$  in a system of many **physical qubits**
- Make use of **symmetry properties (parity)** of logical qubit states
  - revealing errors ...
  - ... but not the encoded quantum state



Kitaev, *Annals of Physics* **303**, 2 (2003),  
Dennis et al., *Journ. of Math. Physics* **43**, 4452 (2002)  
Raussendorff, Harrington, *Phys. Rev. Lett.* **98**, 190504 (2007)  
Fowler et al., *Phys. Rev. A* **86**, 032324 (2012)

# The Surface Code – Main Features

## Large error threshold $\epsilon_{\text{th}} \sim 1\%$

- Logical error rate  $\epsilon_L \propto (\epsilon_{\text{phys}}/\epsilon_{\text{th}})^{(d+1)/2}$   
 $\epsilon_{\text{phys}}$ : Physical error rate per step  
 $\epsilon_{\text{th}}$ : Threshold error rate  
 $d$ : Distance of the code

## Two-dimensional architecture

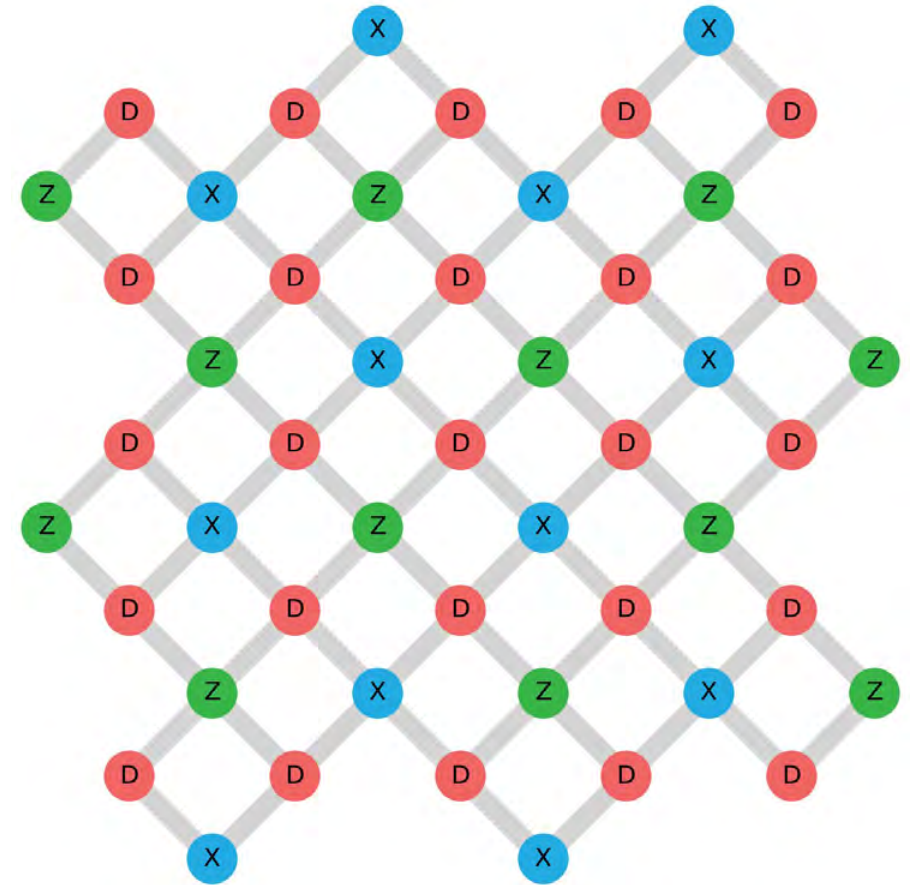
- All operations realizable on a planar qubit lattice
- Topological code: only local operations needed for error correction process

Kitaev, *Annals of Physics* **303**, 2 (2003),

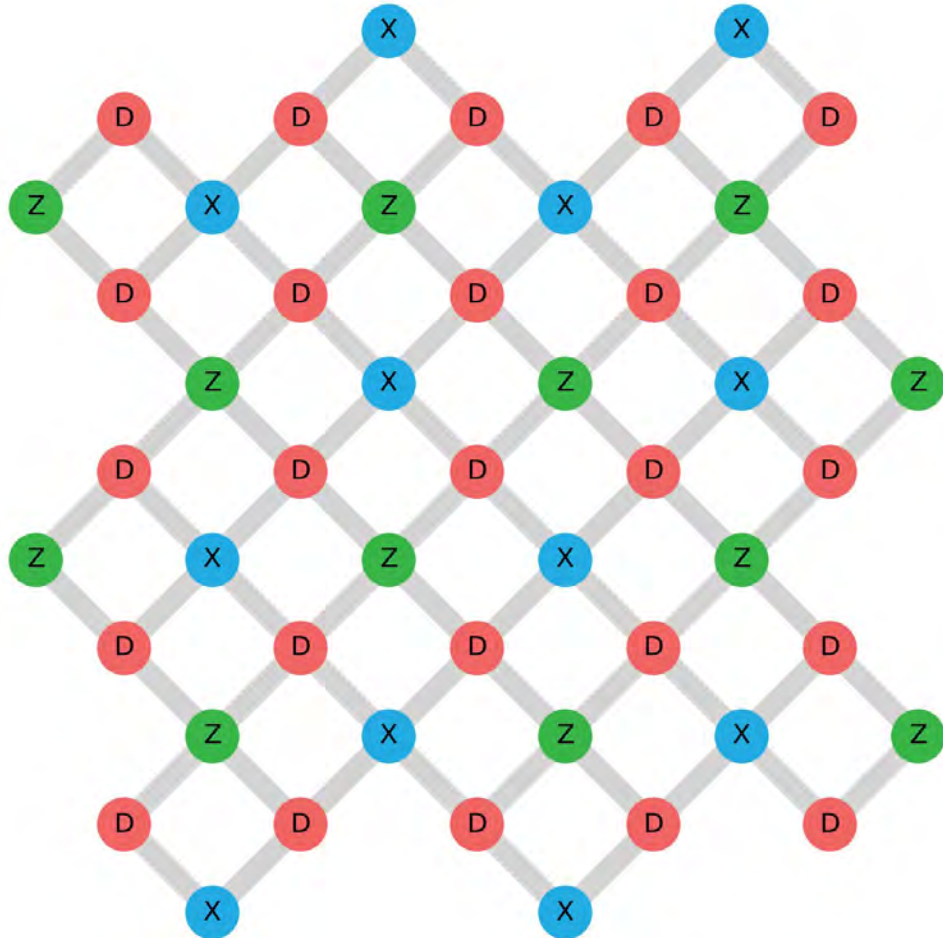
Dennis et al., *Journ. of Math. Physics* **43**, 4452 (2002)

Raussendorff, Harrington, *Phys. Rev. Lett.* **98**, 190504 (2007)

Fowler et al., *Phys. Rev. A* **86**, 032324 (2012)

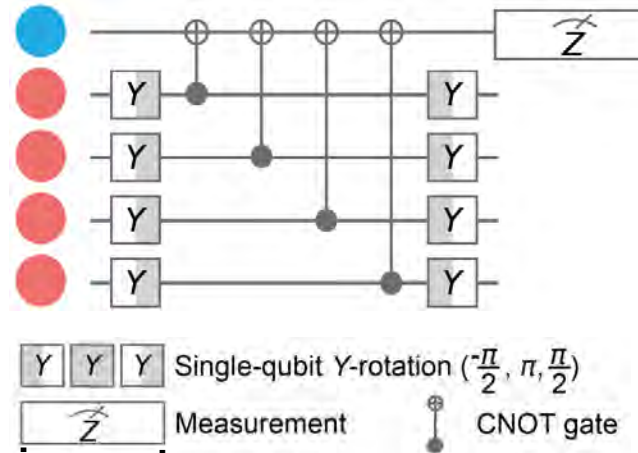


# Elements of the Surface Code



## Features:

- Two-dimensional ( $d \times d$ ) grid of **data qubits**
- **X-type** and **Z-type** auxiliary qubits
- Auxiliary-qubit-assisted stabilizer measurement
  - $Z_1 Z_2 Z_3 Z_4$  (or  $Z_1 Z_2$  at the edges)
  - $X_1 X_2 X_3 X_4$  (or  $X_1 X_2$  at the edges)



## Requirements:

- High-fidelity entangling gates between data and ancilla qubits
- Fast high-fidelity measurements of the ancilla qubits
- Low readout crosstalk between ancilla and data qubits
- Ability to do repeated gates and mid-cycle measurements

Fowler *et al.*, *Phys. Rev. A* **86**, 032324 (2012)

Versluis *et al.*, *Phys. Rev. Applied* **8**, 034021 (2017)

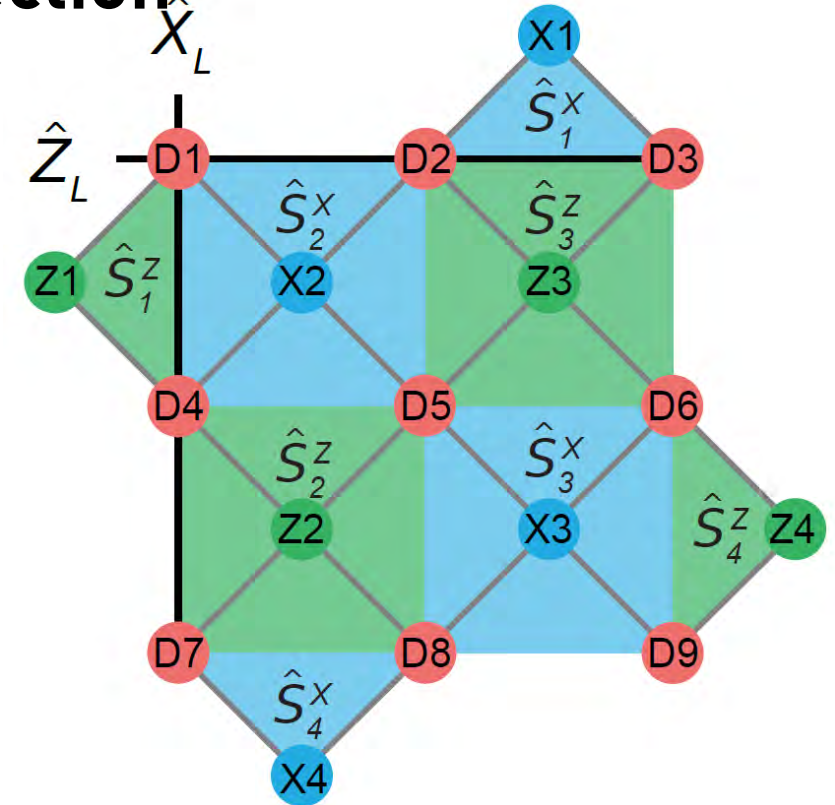
# Distance-Three Surface Code for Error Correction

Two-dimensional square lattice of qubits

- $d^2 = 9$  Data qubits: encode single (logical) qubit
  - Logical operators:  $\hat{Z}_L = \hat{Z}_1 \hat{Z}_2 \hat{Z}_3$     $\hat{X}_L = \hat{X}_1 \hat{X}_4 \hat{X}_7$
  - Distance  $d$ : min. number of Pauli operators in  $\hat{Z}_L, \hat{X}_L$
  - Number of correctable errors:  $\lfloor (d - 1)/2 \rfloor = 1$
- $d^2 - 1 = 8$  Auxiliary qubits: for parity measurements

Parity/Stabilizer measurements

- Detect errors without collapsing data-qubit state (Stabilizer operators commute with  $\hat{Z}_L, \hat{X}_L$ )
- 4 **Z-type Stabilizers**  $\hat{S}^{Zi}$  to detect bit-flip errors
- 4 **X-type Stabilizers**  $\hat{S}^{Xi}$  to detect phase-flip errors



|                |                                           |                |                                           |
|----------------|-------------------------------------------|----------------|-------------------------------------------|
| $\hat{S}^{Z1}$ | $\hat{Z}_1 \hat{Z}_4$                     | $\hat{S}^{X1}$ | $\hat{X}_2 \hat{X}_3$                     |
| $\hat{S}^{Z2}$ | $\hat{Z}_4 \hat{Z}_5 \hat{Z}_7 \hat{Z}_8$ | $\hat{S}^{X2}$ | $\hat{X}_1 \hat{X}_2 \hat{X}_4 \hat{X}_5$ |
| $\hat{S}^{Z3}$ | $\hat{Z}_2 \hat{Z}_3 \hat{Z}_5 \hat{Z}_6$ | $\hat{S}^{X3}$ | $\hat{X}_5 \hat{X}_6 \hat{X}_8 \hat{X}_9$ |
| $\hat{S}^{Z4}$ | $\hat{Z}_6 \hat{Z}_9$                     | $\hat{S}^{X4}$ | $\hat{X}_7 \hat{X}_8$                     |

Bombin, Delgado, *Phys. Rev. A* **76**, 012305 (2007)

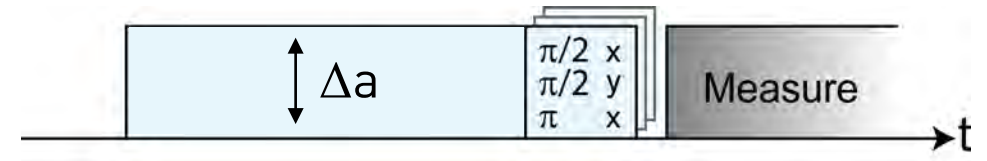
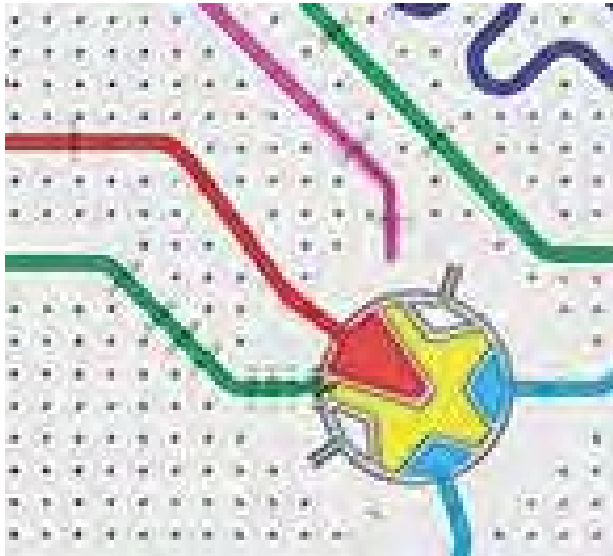
Tomita, Svore, *Phys. Rev. A* **90**, 062320 (2014)

1 mm

QUDEV

# Controlling Single Qubits (Y Rotation)

- apply microwave pulse
- followed by read-out pulse
- both with controlled length, amplitude and phase
- Characterize gates by randomized benchmarking
- $F > 99 \%$

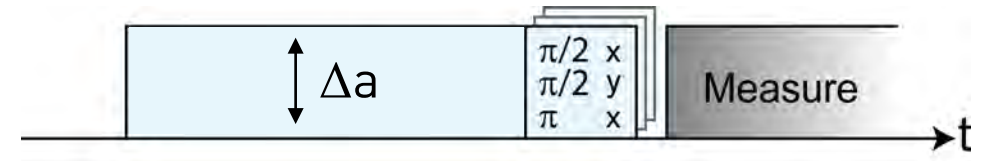


experimental density matrix and Pauli set:



# Controlling Single Qubits (X Rotation)

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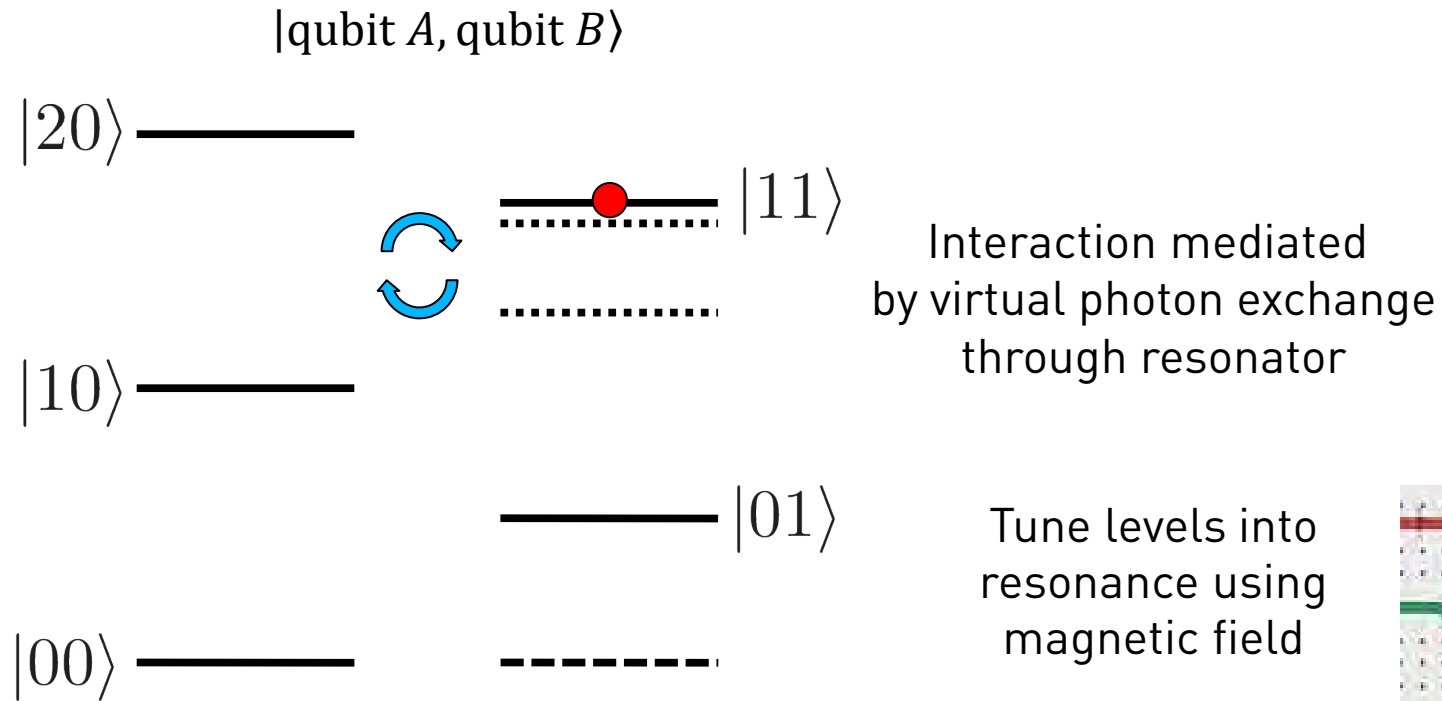


experimental density matrix and Pauli set:



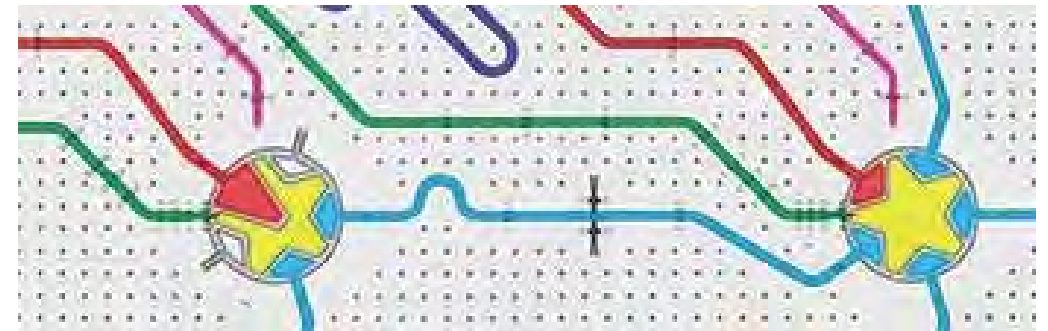
# Universal Two-Qubit Controlled Phase Gate

Make use of qubit states beyond 0, 1



$$|11\rangle \longrightarrow i|20\rangle \longrightarrow -|11\rangle$$

Full  $2\pi$  rotation induces phase factor -1

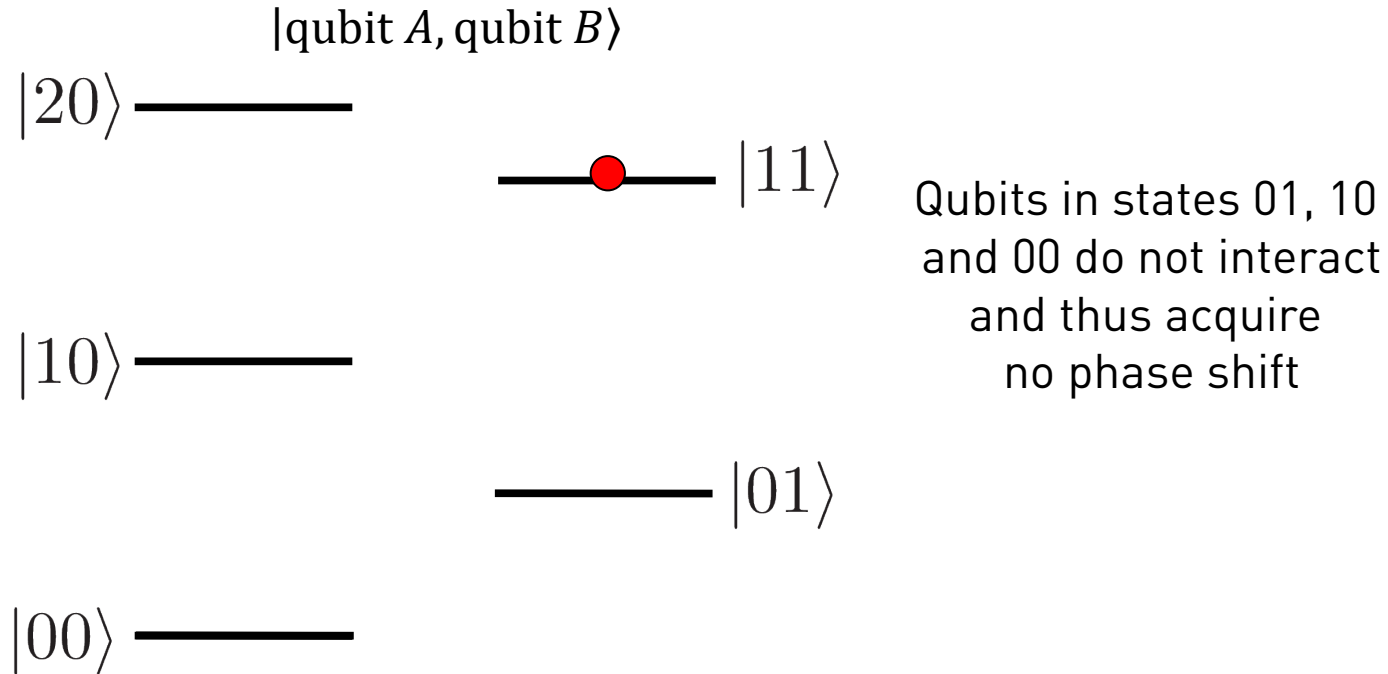


proposal: F. W. Strauch *et al.*, *Phys. Rev. Lett.* **91**, 167005 (2003).

first implementation: L. DiCarlo *et al.*, *Nature* **460**, 240 (2010).

# Universal Two-Qubit Controlled Phase Gate

Make use of qubit states beyond 0, 1



Universal two-qubit gate.

Test performance with process tomography or randomized benchmarking.

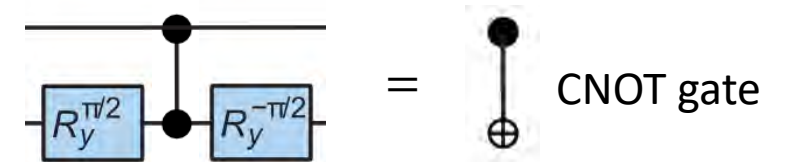
proposal: F. W. Strauch *et al.*, *Phys. Rev. Lett.* **91**, 167005 (2003).

first implementation: L. DiCarlo *et al.*, *Nature* **460**, 240 (2010).

$$\begin{aligned}
 |11\rangle &\longrightarrow i|20\rangle \longrightarrow -|11\rangle \\
 |01\rangle &\longrightarrow |01\rangle \\
 |10\rangle &\longrightarrow |10\rangle \\
 |00\rangle &\longrightarrow |00\rangle
 \end{aligned}$$

C-Phase gate:

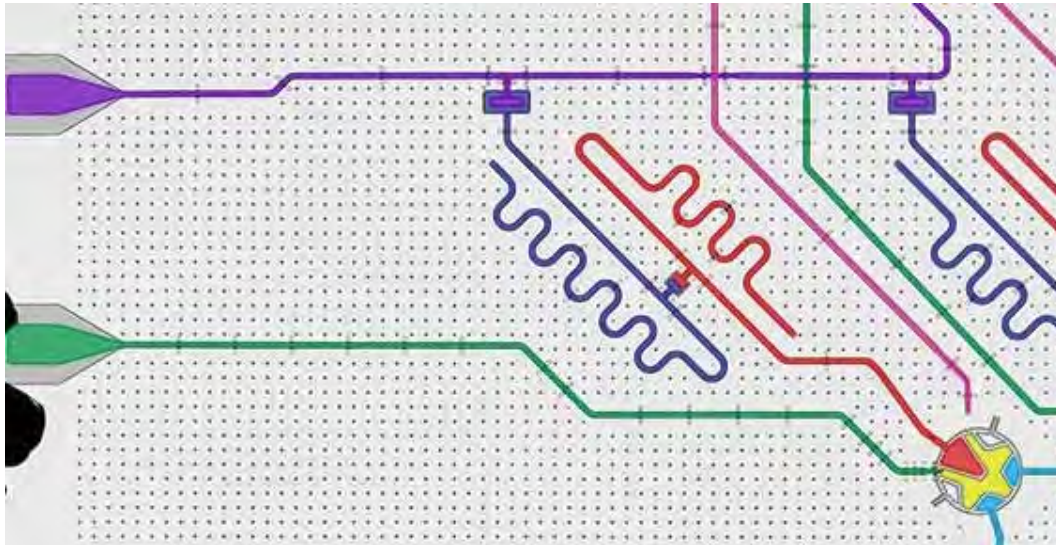
$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$



# Qubit Readout

## Circuit design

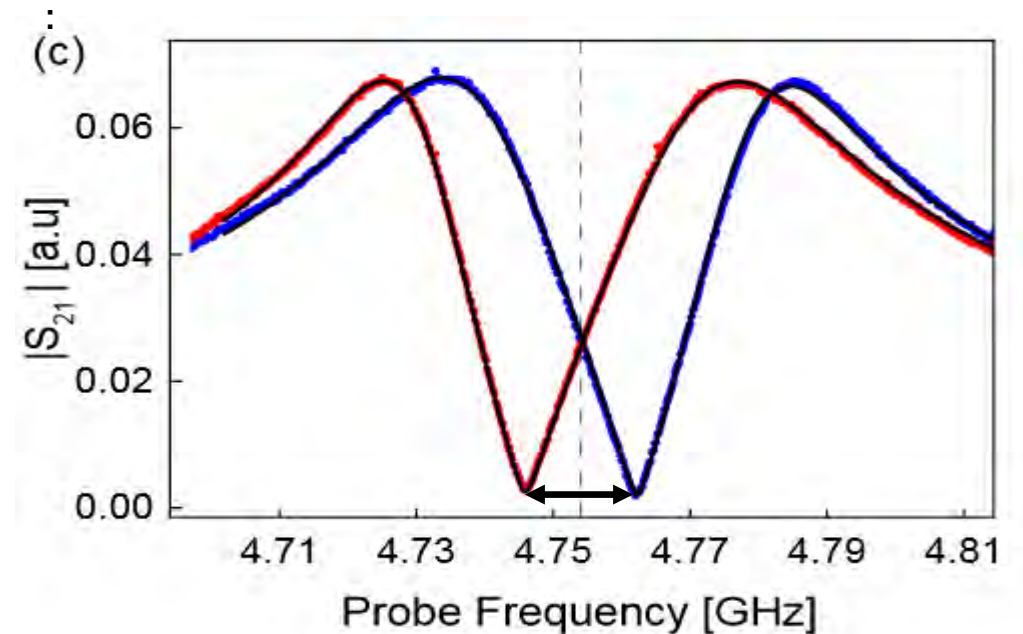
- $\lambda/4$  readout resonator &  $\lambda/4$  Purcell filter



## Performance

- $F \sim 99.2\%$  at 88 ns integration time
- Optimized sample design
- Low-noise phase-sensitive JP-Amplifier

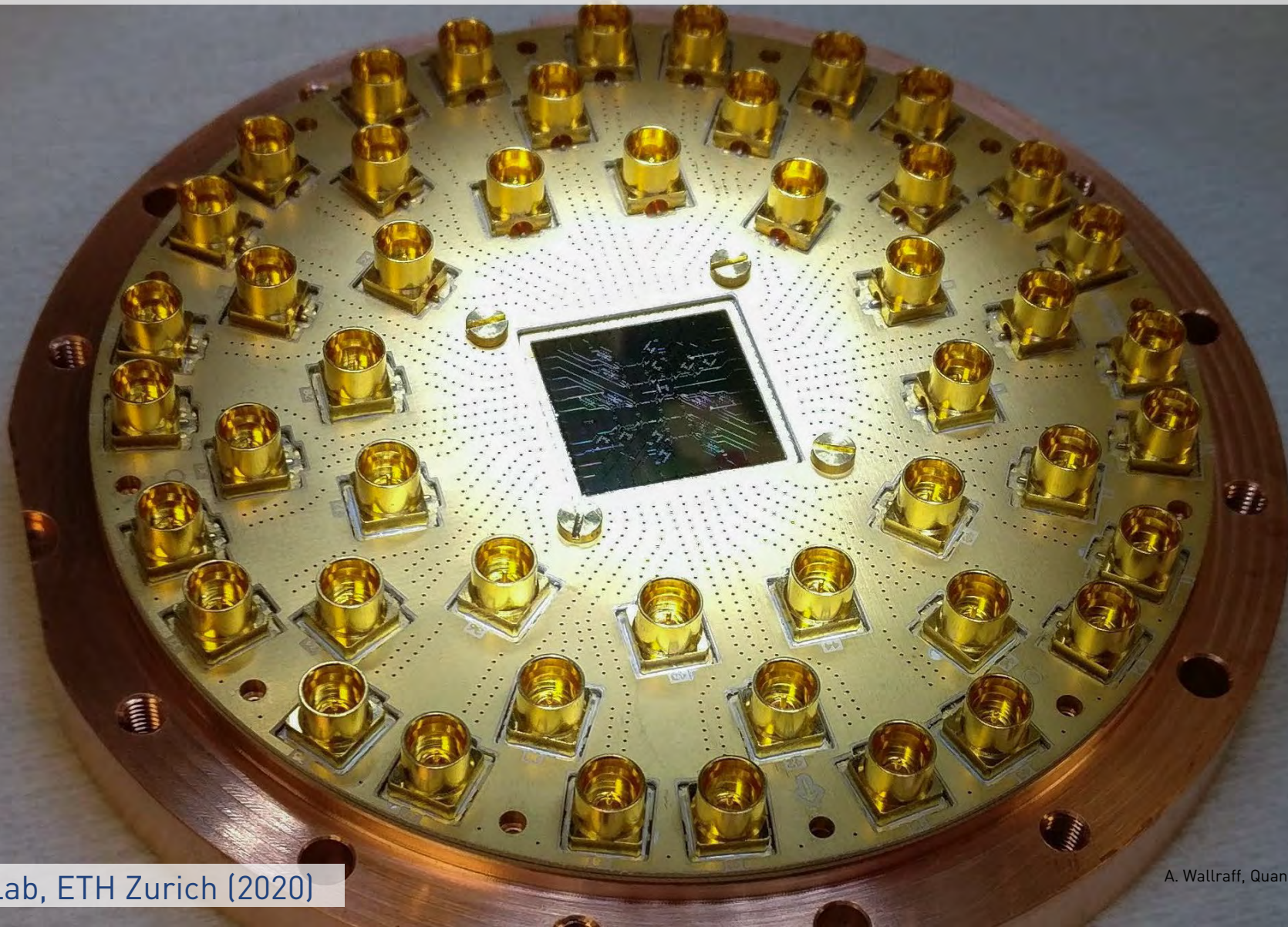
Transmission amplitude of readout circuit for qubit prepared in **ground (g)** or **excited (e)** state



## Features:

- large dispersive shift  $\chi$
- large resonator BW  $\kappa$
- Purcell protection
- Low cross-talk when multiplexed

# Distance-Three Surface-Code Device Mounted in Sample Holder



# 48-Port Sample Package (17-Qubit Device)

Quantum Device Lab,  
ETH Zurich (2020)





# Qubit-Encoded Quantum Error Correction Experiments

## Bit or phase-flip codes (only X or Z errors):

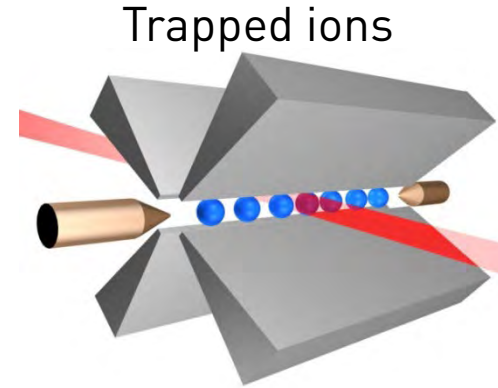
- NMR [Cory et al. Phys. Rev. Lett. 81, 2152 (1998)]
- Ions [Chiaverini et al. Nature 432, 602 (2004), Schindler et al. Science 322, 1059 (2011)]
- NV-Centers [Cramer et al. Nature Comm. 7, 11526 (2016)]
- Superconducting qubits [Riste et al. Nature Comm. 6, 6983 (2015), Kelly et al. Nature 519, 66 (2015), Chen et al., Nature 595, 7867 (2021)]

## Quantum codes, single-cycle experiments:

- Five-qubit code [Knill et al., PRL 86, 5811 (2001), Abobeih et al., arXiv:2108.01646 (2021)]
- Bacon-Shor code [Egan et al., Nature 598, 281 (2021)]

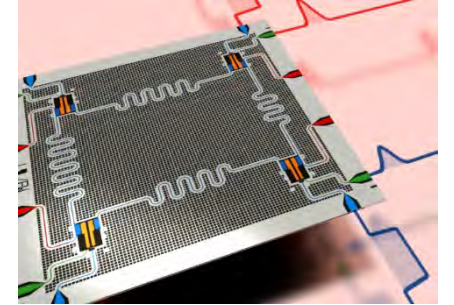
## Repeated error detection in the surface code

- Andersen et al., Nat. Phys. 16, 875 (2020)
- Chen et al., Nature 595, 7867 (2021)
- Marques et al., Nat. Phys. 18, 80 (2022)



Trapped ions  
e.g. Blatt & Roos, Nat. Phys. 8, 277 (2012)

## Supercond. circuits



Picture: Y. Salathé  
Review: e.g. Krantz et al., Appl. Phys. Rev. 6, 021318 (2019)

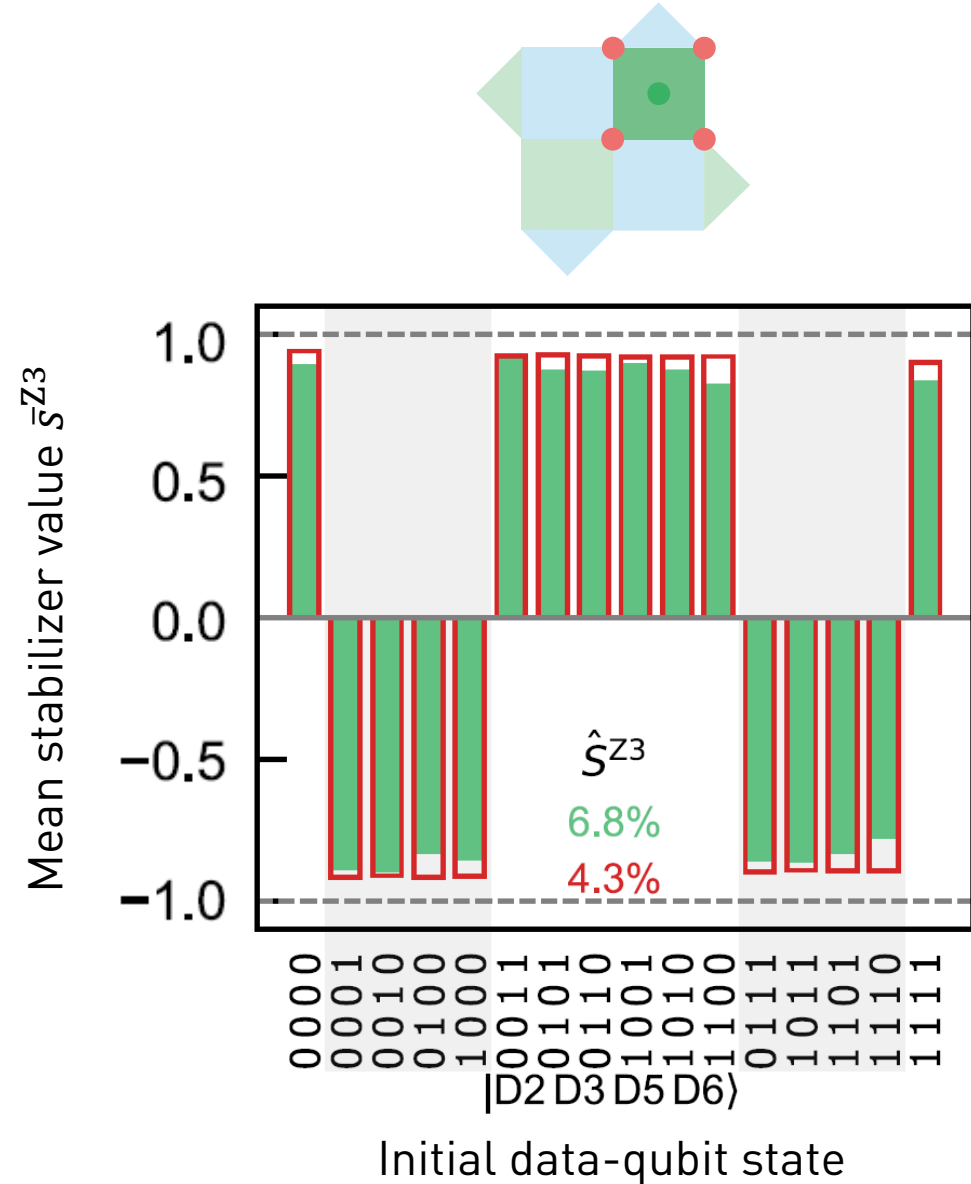
## Repeated quantum error correction

- Color code (trapped ions) Ryan-Anderson et al., PRX 11, 041058 (2021)
- Distance-3 surface code (s.c.) Krinner, Lacroix et al., Nature 605, 669 (2022) Zhao et al., PRL 129, 030501 (2022)
- Distance-3 heavy-hexagon code (s.c.) Sundaresan et al., Nat. Commun. 14, 2852 (2023)
- Distance-3 to 5 scaling of the surface code (s.c.) Google AI, Nature 614, 676 (2023)

# Stabilizer Characterization

## Individual characterization

- Prepare data qubits of plaquette in all 4 (weight-2) or 16 (weight-4) basis states
- Stabilizer execution yields  $s^{Ai} = \pm 1$
- Average over  $\sim 4 \times 10^4$  measurements to obtain  $\bar{s}^{Ai}$
- Measured and calculated error



# Stabilizer Characterization

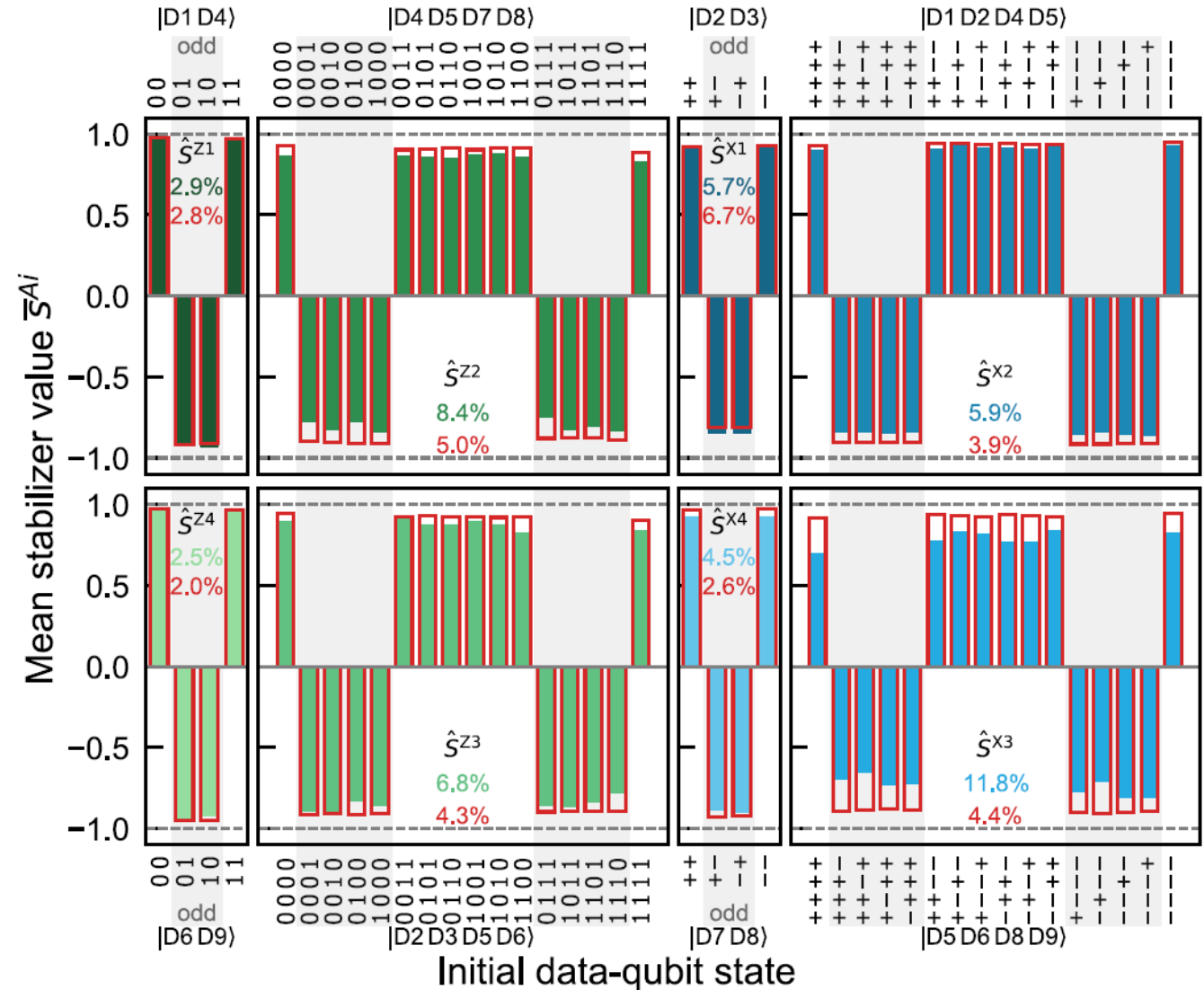
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- Stabilizer execution yields  $s^{Ai} = \pm 1$
- Average over  $\sim 4 \times 10^4$  measurements to obtain  $\bar{s}^{Ai}$
- Measured and calculated error

## Average parity error

- Weight-2 stabilizers: 3.9(1.3) %
- Weight-4 stabilizers: 8.2(2.2) %

Qualitative agreement with master-equation simulations

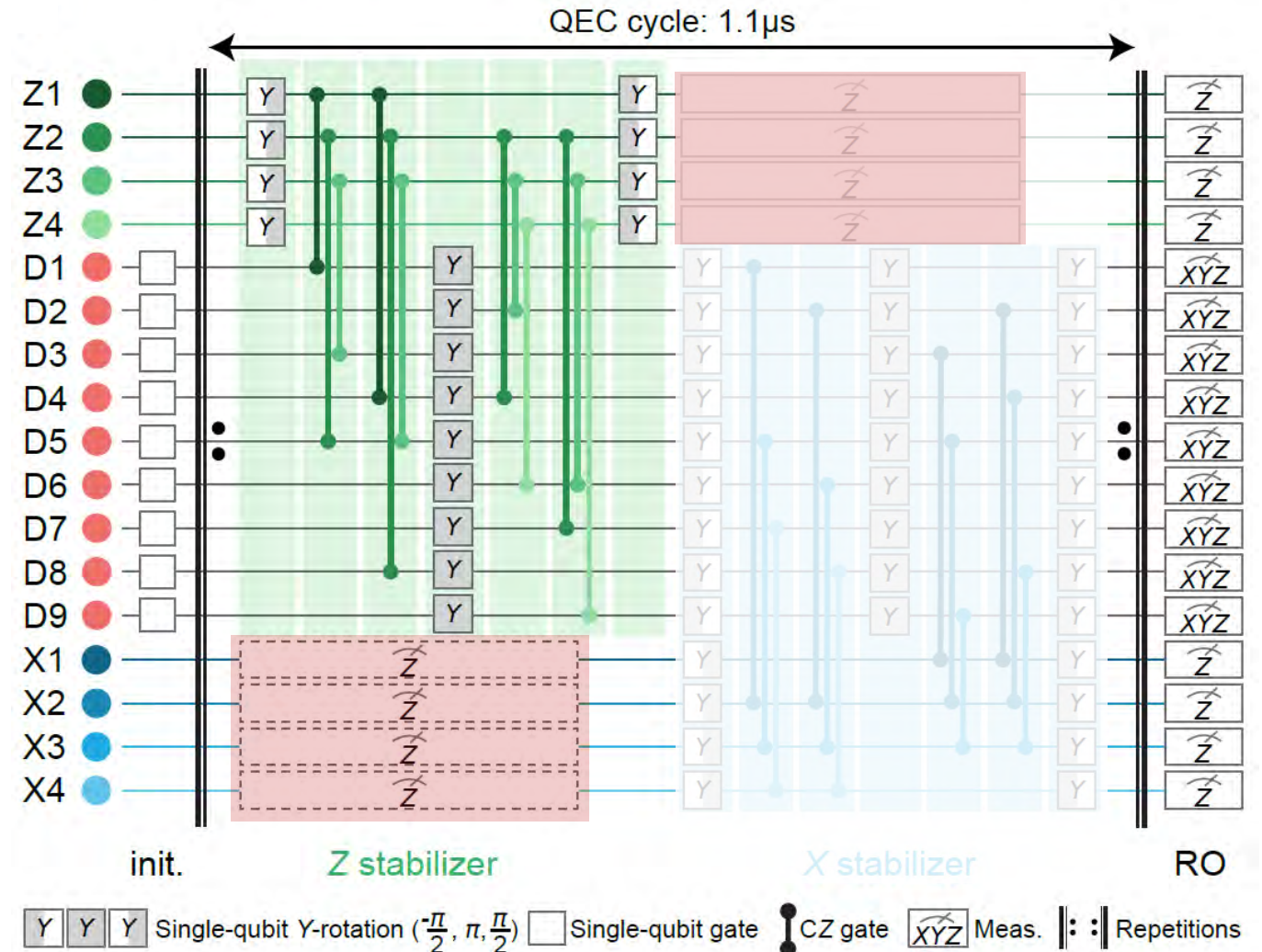


# The Surface Code Cycle

- All four  $\hat{S}^{Zi}$  measured in parallel
- All four  $\hat{S}^{Xi}$  measured in parallel
- Pipelining: **Read out** one stabilizer type while running gates of the other.
- Logical state preparation:  $|0\rangle_L$ ,  $|1\rangle_L$  and  $|\pm\rangle_L = (|0\rangle_L \pm |1\rangle_L)/\sqrt{2}$  in single cycle.
- State preservation over n cycles
  - Cycle duration: 1.1  $\mu\text{s}$
  - Leakage detection and rejection executed in every cycle
  - circuits with  $\sim 800$  single-qubit gates and  $\sim 400$  two-qubit gates

Versluis et al., *PR Applied* **8**, 034021 (2017)

S. Krinner, N. Lacroix et al., *Nature* **605**, 669 (2022)



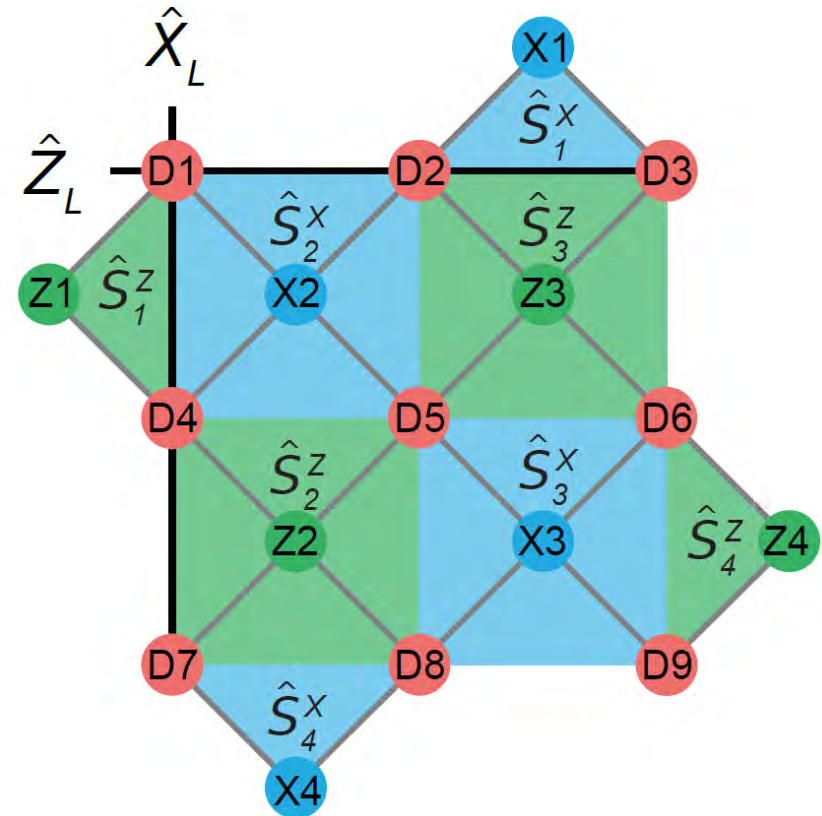
# Repeated Quantum Error Correction

## Measurement of Logical Z and Logical X Operators

- Initialization
  - $|0\rangle_L$ : prepare data qubits in  $|0\rangle^{\otimes 9}$
  - $|1\rangle_L$ : prepare data qubits in  $X_L|0\rangle^{\otimes 9}$
  - $|+\rangle_L$ : prepare data qubits in  $|+\rangle^{\otimes 9}$
  - $|-\rangle_L$ : prepare data qubits in  $Z_L|+\rangle^{\otimes 9}$
- Perform  $n$  QEC cycles
- Read out all data qubits in Z-basis (X-basis)

## Analysis

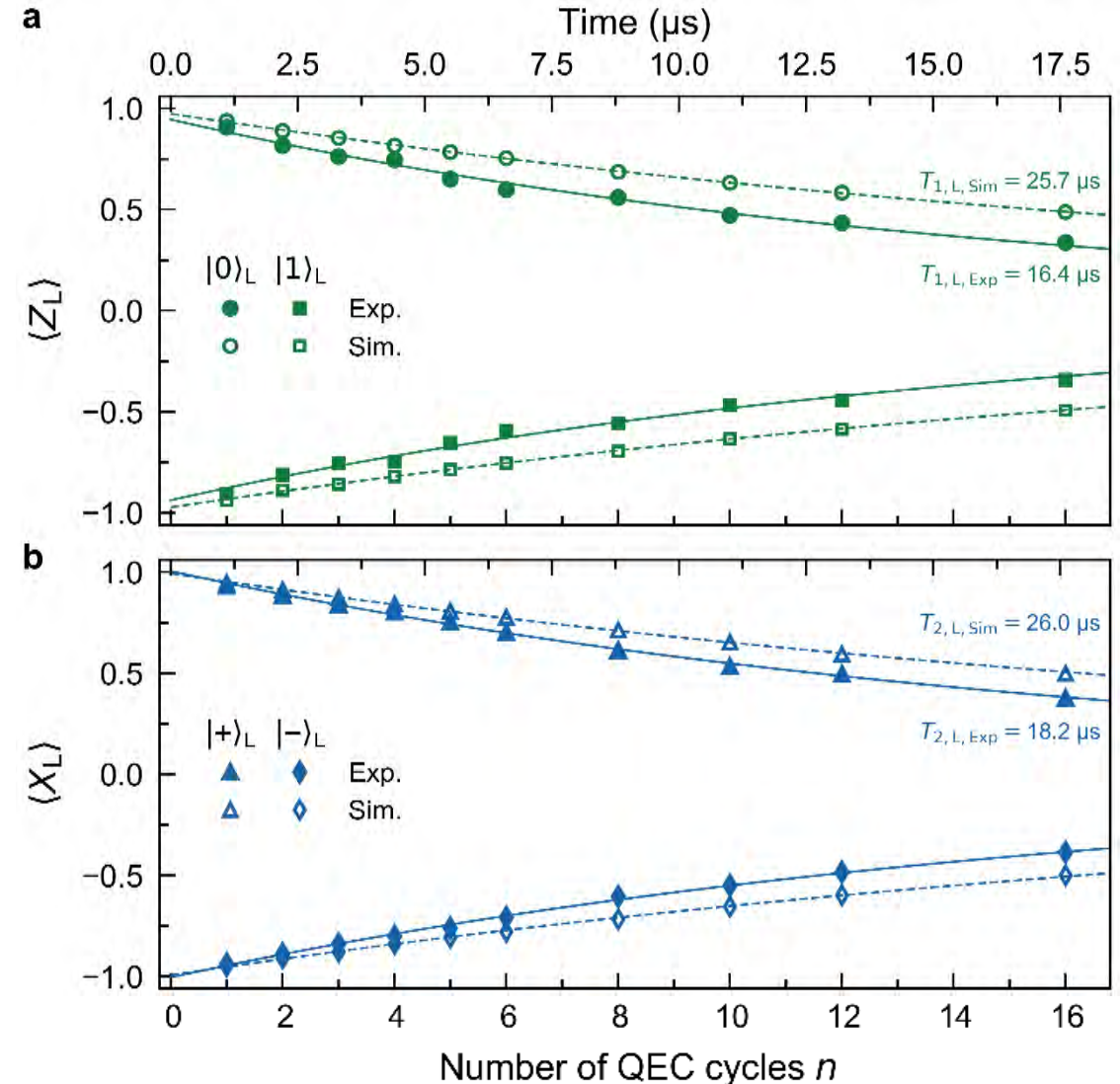
- Determine logical operator  $z_L = z_1 z_2 z_3 = \pm 1$  ( $x_L = x_1 x_4 x_7 = \pm 1$ ) for each run with up to  $n$  repeated cycles
- Apply correction conditioned on decoded syndromes for each run
- Average over runs with  $n$  repeated cycles to compute  $\bar{z}_L = \langle \hat{Z}_L \rangle$  ( $\bar{x}_L = \langle \hat{X}_L \rangle$ )



# Repeated Quantum Error Correction

## Outcomes Logical Z and Logical X

- Exponential decay of logical expectation values
- Logical lifetime  
 $T_{1,L} = 16.4(8) \mu\text{s} \gg t_c = 1.1 \mu\text{s}$
- Logical coherence time  
 $T_{2,L} = 18.2(5) \mu\text{s} \gg t_c = 1.1 \mu\text{s}$
- Master equation simulation of logical lifetimes of  $\sim 26 \mu\text{s}$  provide upper bound for achievable lifetimes with our device performance



# Logical Error Probability and Logical Error per Cycle

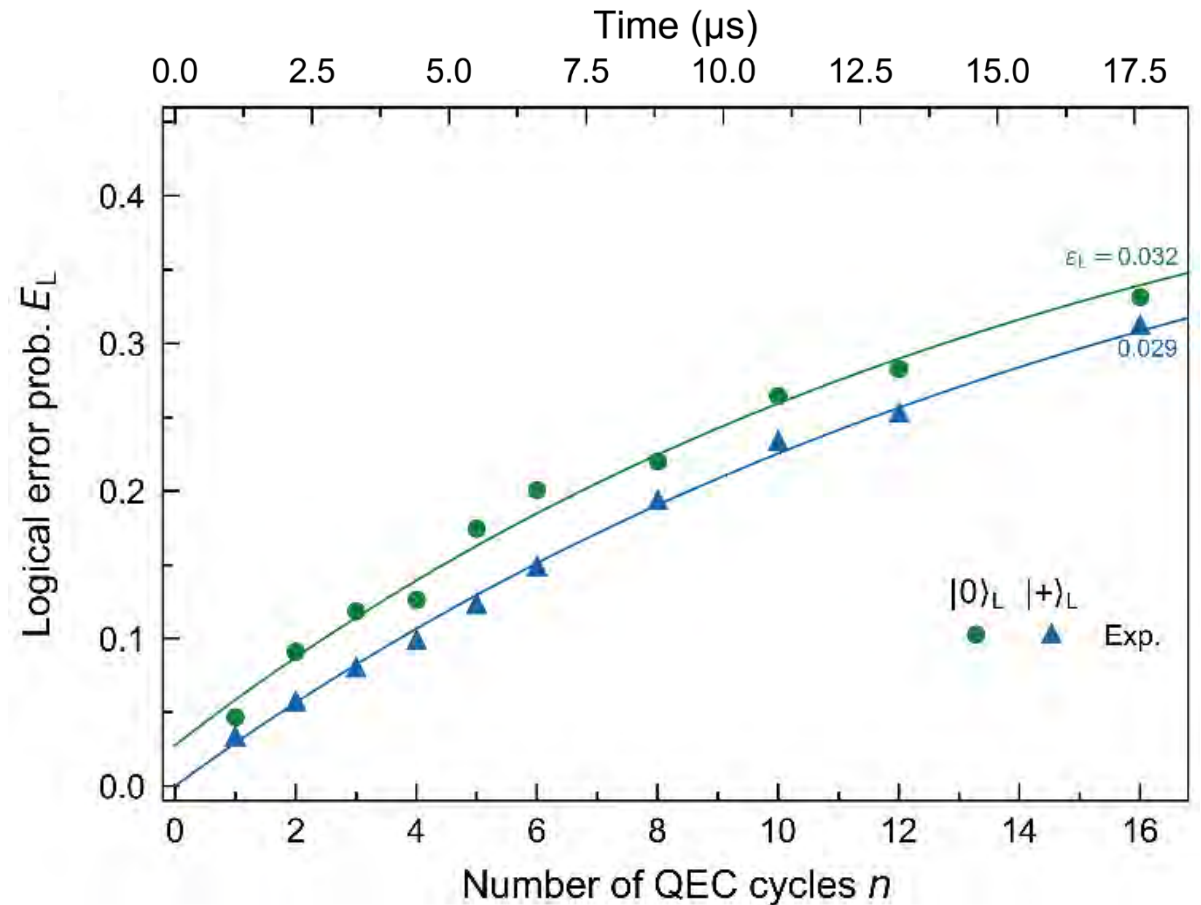
Logical error probability:

- $E_L = (1 - \langle \hat{Z}_L \rangle)/2$  for eigenstates of  $\hat{Z}_L$
- $E_L = (1 - \langle \hat{X}_L \rangle)/2$  for eigenstates of  $\hat{X}_L$

Logical error per cycle:

- Extracted from fit to  $E_L(n)$  or from  $T_{1/2,L}$ :  

$$\epsilon_L = \frac{1}{2} [1 - \exp(-t_c/T_{1/2,L})] \approx t_c/2T_{1/2,L}$$
- $\epsilon_L \sim 0.03$



# Repeated Quantum Error Correction with $d \geq 3$ Codes

Published work:

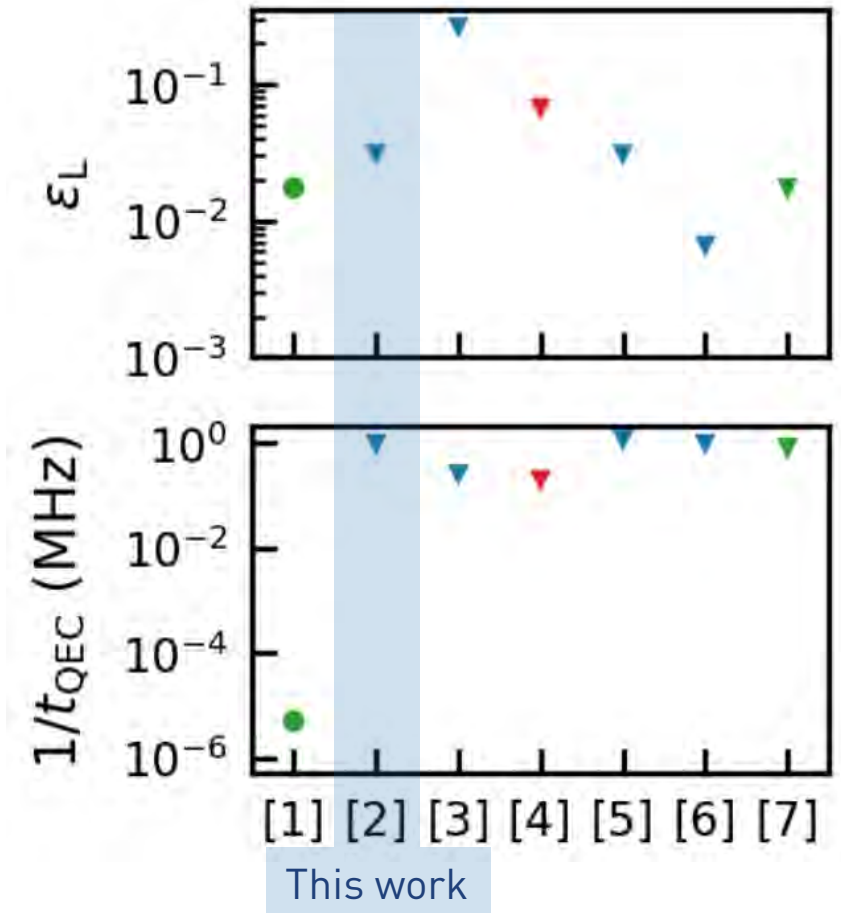
- Honeywell: [1] Ryan-Anderson *et al.*, *Phys. Rev. X* **11**, 041058 (2021)
- ETHZ: [2] Krinner, Lacroix *et al.*, *Nature* **605**, 669 (2022)
- USTC: [3] Zhao *et al.*, *PRL* **129**, 030501 (2022)
- IBM: [4] Sundaresan *et al.*, *Nat. Commun.* **14**, 2852 (2023)
- Google: [5] Google Quantum AI, *Nature* **614**, 676 (2023)
- Google: [6] Google Quantum AI, *Nature* **638**, 920 (2025)
- Google: [7] Lacroix *et al.*, *Nature* (2025)

Implementations:

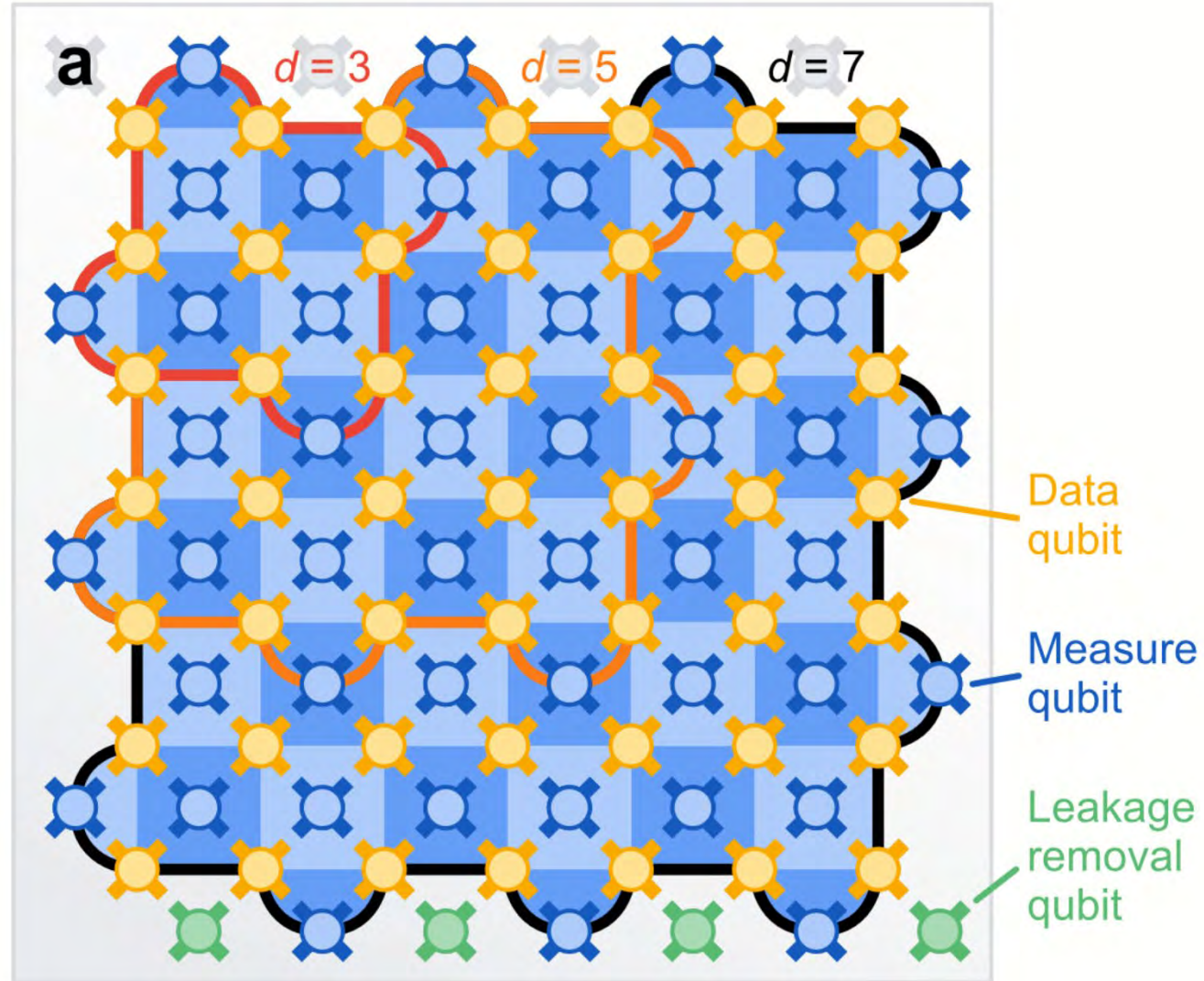
- superconducting-circuits ( $\nabla$ ) and trapped-ions (0)
- Color code, surface code and heavy-hexagon code

Performance criteria

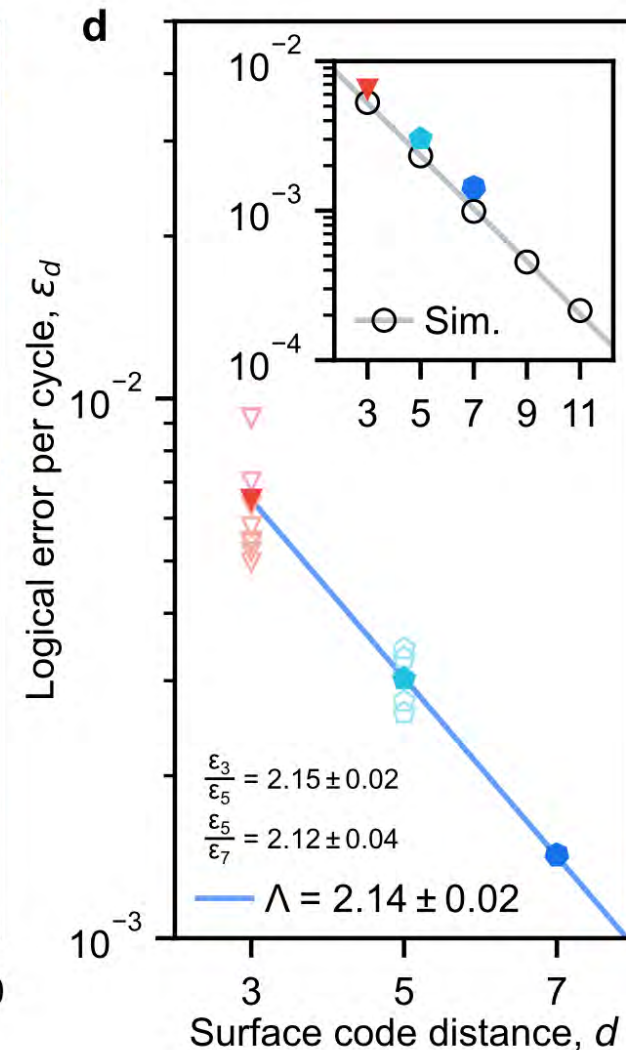
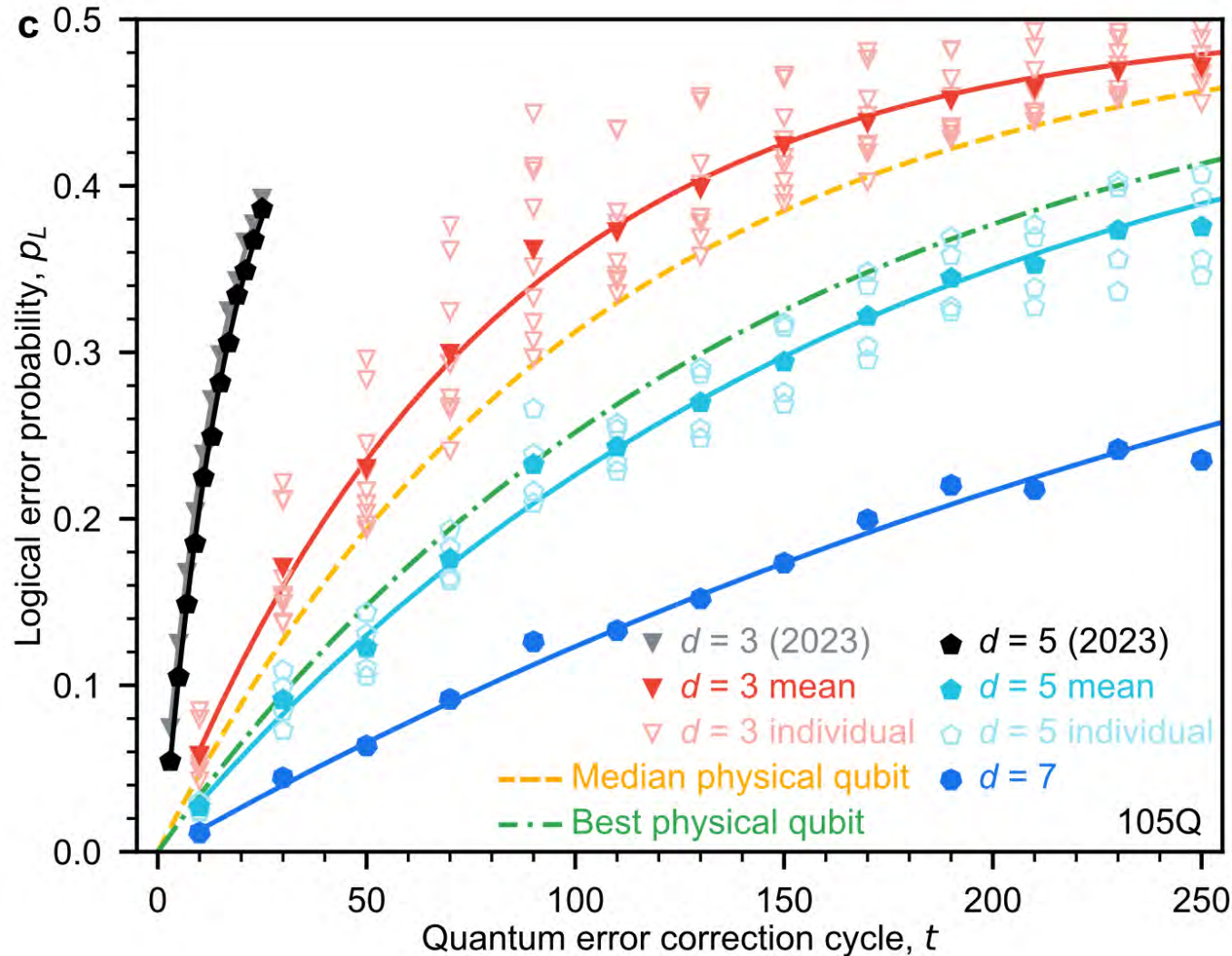
- Small logical error per cycle  $\epsilon_L$
- High QEC cycle rate  $1/t_{\text{QEC}}$



# Distance-Three, -Five and -Seven Surface Code Layout



# Distance Scaling and Logical Error Suppression

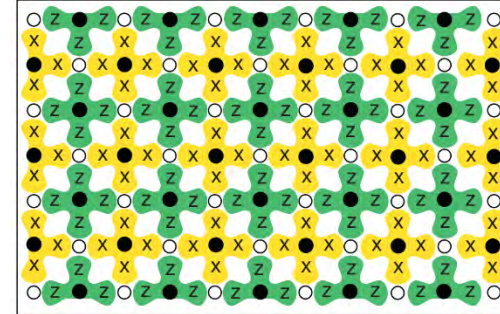


# Surface Code and Lattice Surgery

- Surface code promising candidate for implementation of logical qubits in superconducting circuits

Kitaev, A. Ann. Phys. 303 1 (2003)

Fowler, A. et al. Phys. Rev. A 86, 032324 (2012)

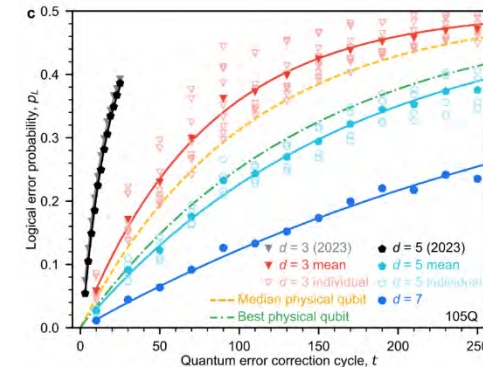


- Experimental realizations of logical state preservation near and beyond the threshold

Krinner, S. et al. Nature 605, pages 669–674 (2022)

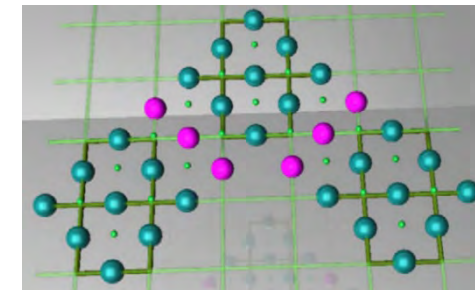
Google Quantum AI, Nature 614, pages 676–681 (2023)

Google Quantum AI and Collaborators, Nature (2024)



- Lattice surgery allows realization of non-transversal interactions between encoded qubits with low qubit-overhead

Horsman, D. et al. New J. Phys. 14 123011 (2012)



# Experimental Work on Logical Qubit Operations

## Logical operations on **encoded qubits**:

- Fault-tolerant subset of Clifford group on  $[4,2,2]$  code (s.c.)  
Harper, R. et al. Phys. Rev. Lett. **122**, 080504 (2019)
- Transversal CNOT on two  $[7,1,3]$  color codes (ions)  
Postler, L. et al. Nature **605**, 675 (2022)

## Non-fault-tolerant **arbitrary state preparation**

- $d = 3$  Bacon-Shor code (ions)  
Egan, L. et al. Nature **598**, 281 (2021)
- $d = 3$  surface code (s.c.)  
Ye, Y. et al. Phys. Rev. Lett. **131**, 210603 (2023)

## Lattice surgery ...

- ... on a  $d = 2$  surface code (ions)  
Erhard, A. et al. Nature **589**, 220 (2021)
- ... on interleaved  $d = 3$  3CX and Bacon-Shor code (s.c.)  
Hetenyi, B. et al. PRX Quantum **5**, 040334 (2024)
- ... on a  $d = 3$  color code (s.c.)  
Lacroix, N. et al., Nature (2025)

## **Independent logical qubits** during idling (modularity):

- transversal implementation of various QEC codes (ryd.)  
Bluvstein, D. et al. Nature **626**, 58 (2024)
- state teleportation on three  $d = 3$  color codes (ions)  
Ryan-Anderson, C. et al. Science **385**, 1327 (2024)

Here: Modular lattice surgery on surface code with partial decoding  
from repeated syndrome extraction on superconducting qubits

# Transversal Gates vs. Lattice Surgery

All-to-all connectivity (ions, Rydberg atoms)

- Allows for transversal logical two-qubit gates

2D square lattice connectivity (s.c.)

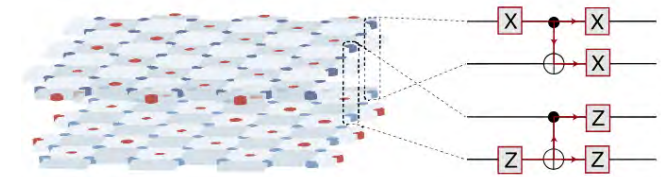
- Requires lattice surgery

Lattice surgery operations:

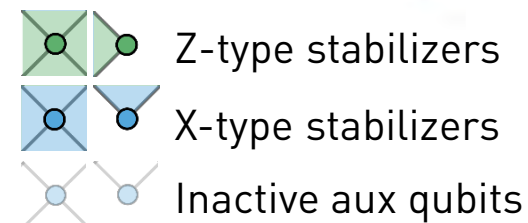
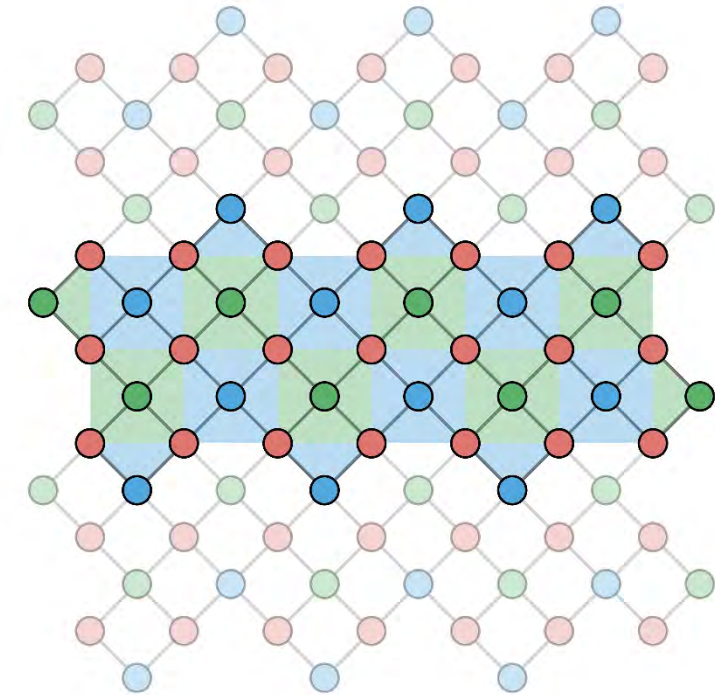
- Merge
- Split
- Measurement of logical two-qubit observables  $\hat{X}_{L1}\hat{X}_{L2}$  (or  $\hat{Z}_{L1}\hat{Z}_{L2}$ )

Horsman, D. et al. New J. Phys. **14** 123011 (2012)

Austin G. Fowler, Craig Gidney arXiv:1808.06709 (2018)



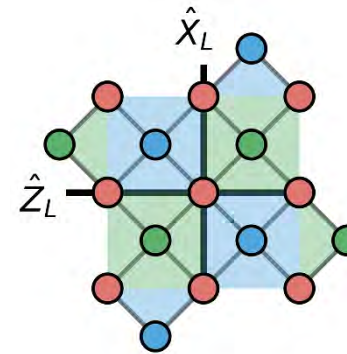
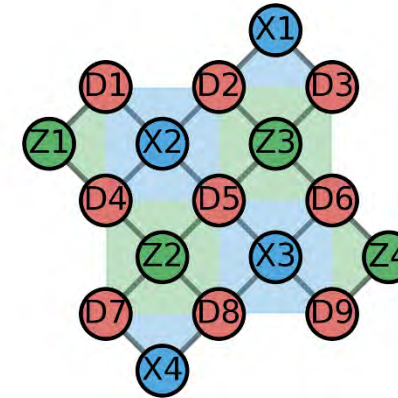
D. Bluvstein et al, Nature **626**, pages 58–65 (2024)



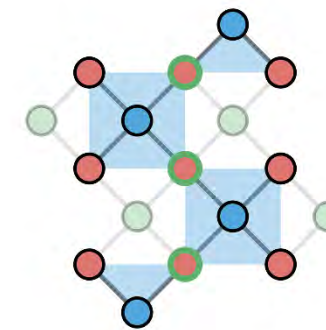
● Data qubit  
● Data qubit (inactive)

# Logical Operators of the Surface and the Repetition Codes

- Distance-three surface code qubit:
  - $3 \times 3$  patch on the data qubit lattice,
  - single bit-flip and phase-flip errors correctable
  - Logical operator definitions
- Lattice split operation transforms the  $d = 3$  surface code into two  $d = 3$  bit-flip codes:
  - Stop measuring X-type stabilizers
  - Readout of middle column of data qubits in Z-basis 
- Two  $d = 3$  bit-flip repetition codes:
  - Two  $1 \times 3$  patches
  - Single bit-flip error correctable
  - Logical operator definitions



$$\begin{aligned}\hat{Z}_L &= \hat{Z}_{D4} \hat{Z}_{D5} \hat{Z}_{D6} \\ \hat{X}_L &= \hat{X}_{D2} \hat{X}_{D5} \hat{X}_{D8} \\ \hat{Y}_L = \hat{Z}_L \hat{X}_L &= \hat{X}_{D2} \hat{Z}_{D4} \hat{Y}_{D5} \hat{Z}_{D6} \hat{X}_{D8}\end{aligned}$$



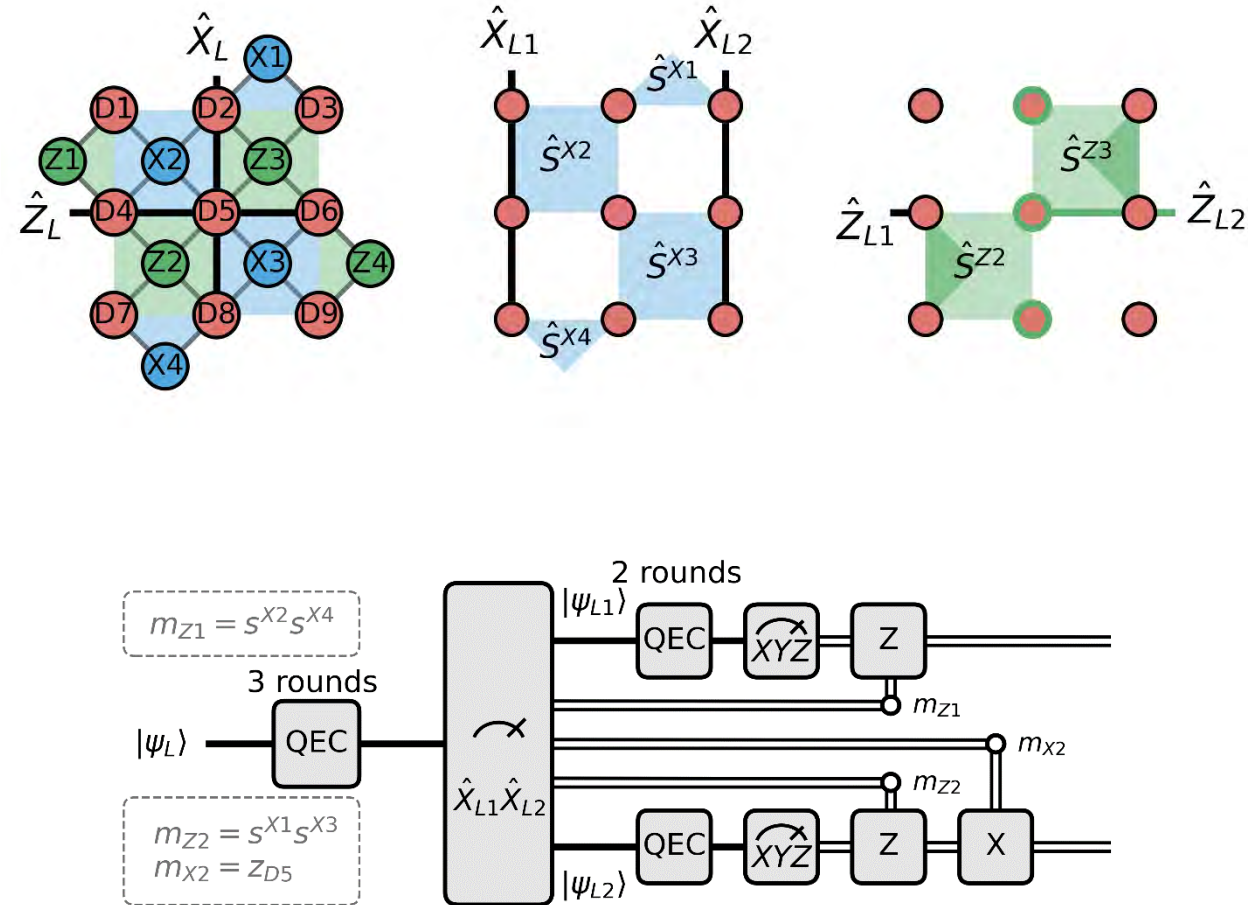
$$\begin{aligned}\hat{Z}_{L1} &= \hat{Z}_{D4} \\ \hat{X}_{L1} &= \hat{X}_{D1} \hat{X}_{D4} \hat{X}_{D7} \\ \hat{Y}_{L1} &= \hat{X}_{D1} \hat{Y}_{D4} \hat{X}_{D7}\end{aligned}$$

$$\begin{aligned}\hat{Z}_{L2} &= \hat{Z}_{D6} \\ \hat{X}_{L2} &= \hat{X}_{D3} \hat{X}_{D6} \hat{X}_{D9} \\ \hat{Y}_{L2} &= \hat{X}_{D3} \hat{Y}_{D6} \hat{X}_{D9}\end{aligned}$$

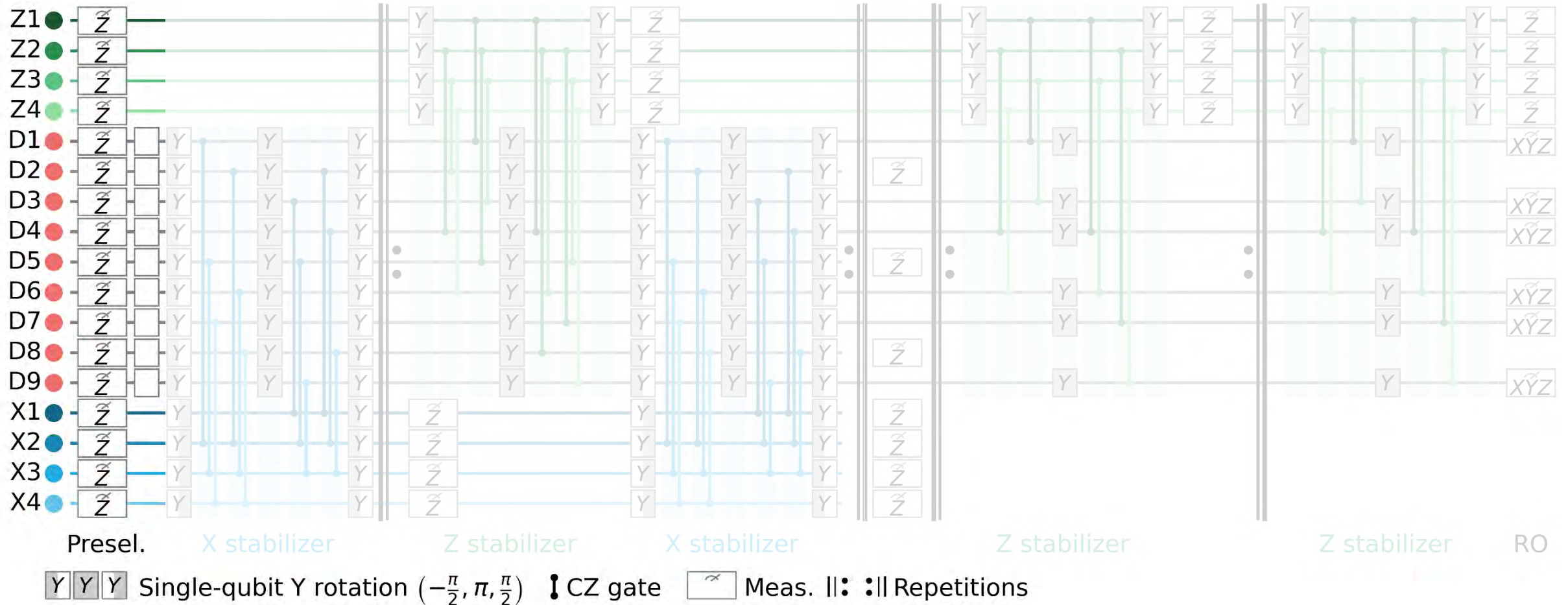
# Pauli Frame Update

- Logical states after split depend on measurement outcomes
- Relation between repetition and surface code logical operators
  - Logical X-operators:
 
$$\hat{X}_{L1} = \hat{X}_L \hat{S}^{X2} \hat{S}^{X4}$$

$$\hat{X}_{L2} = \hat{X}_L \hat{S}^{X1} \hat{S}^{X3}$$
  - Logical Z-operators:
 
$$\hat{Z}_L = \hat{Z}_{D4} \hat{Z}_{D5} \hat{Z}_{D6} = \hat{Z}_{L1} (\hat{Z}_{L2} \hat{Z}_{D5})$$
- Deterministic operation realized by feed-forward Pauli-Frame update:
  - $\hat{X}_L \rightarrow \hat{X}_{L1}, \hat{X}_{L2}$
  - $\hat{Z}_L \rightarrow \hat{Z}_{L1} \hat{Z}_{L2}$
  - performed in post-processing
- Weight-4 Z-type stabilizers become weight-2, value updated by data qubit readout outcome



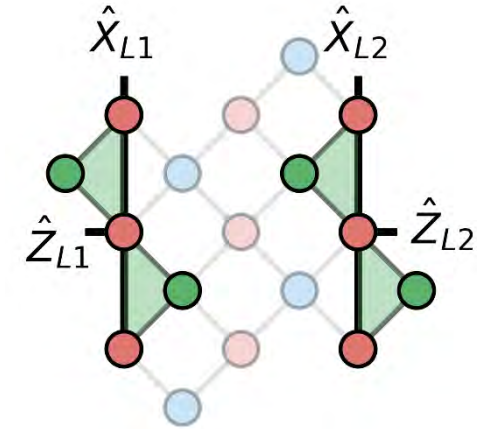
# Gate Sequence of Lattice-Split Operation



- **Qubit initialization**
- **X-syndrome extraction to initialize  $d = 3$  qubit**
- **Three rounds of syndrome extraction**
- **Lattice split**
- **Two rounds of syndrome extraction**
- **Logical observable readout**

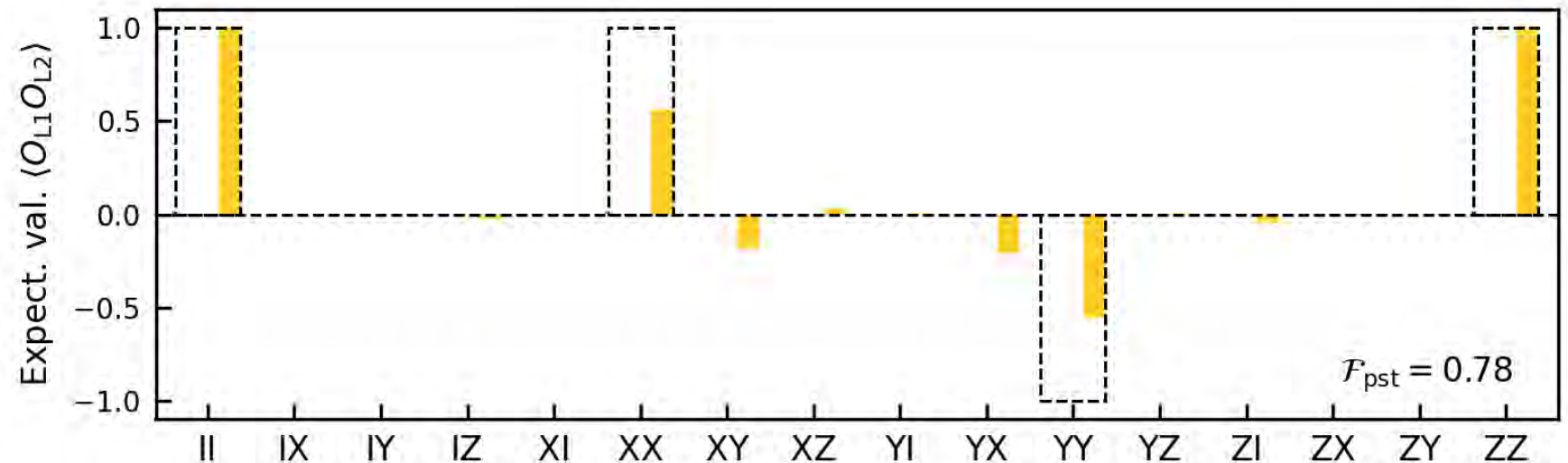
# Logical Bell State Creation

- Prepare surface-code  $|0\rangle_L$  and perform lattice split
- Fault-tolerant ( $d = 3$ ) with respect to **bit-flip errors**
- Non-fault-tolerant ( $d = 1$ ) with respect to **phase-flip errors**
- Evaluate Logical Bell state after **Pauli-frame update**:
  - Ideally  $X_{L1}X_{L2} = Z_{L1}Z_{L2} = 1$  and  $Y_{L1}Y_{L2} = -1$
- ~70'000 shots per logical operator, reject leakage, and calculate **expectation values**



# Logical State Tomography

- Measure **all nine basis combinations of repetition code logical qubits** to perform **logical quantum state tomography**
- Use extracted syndromes to **post-select** on zero syndrome elements (no error)
  - $Z_{L1}Z_{L2}$  error <1%:  
**fault tolerant** with respect to **bit-flips**
  - Expectation value of  $X_{L1}X_{L2}$  and  $Y_{L1}Y_{L2}$  limited by repetition code

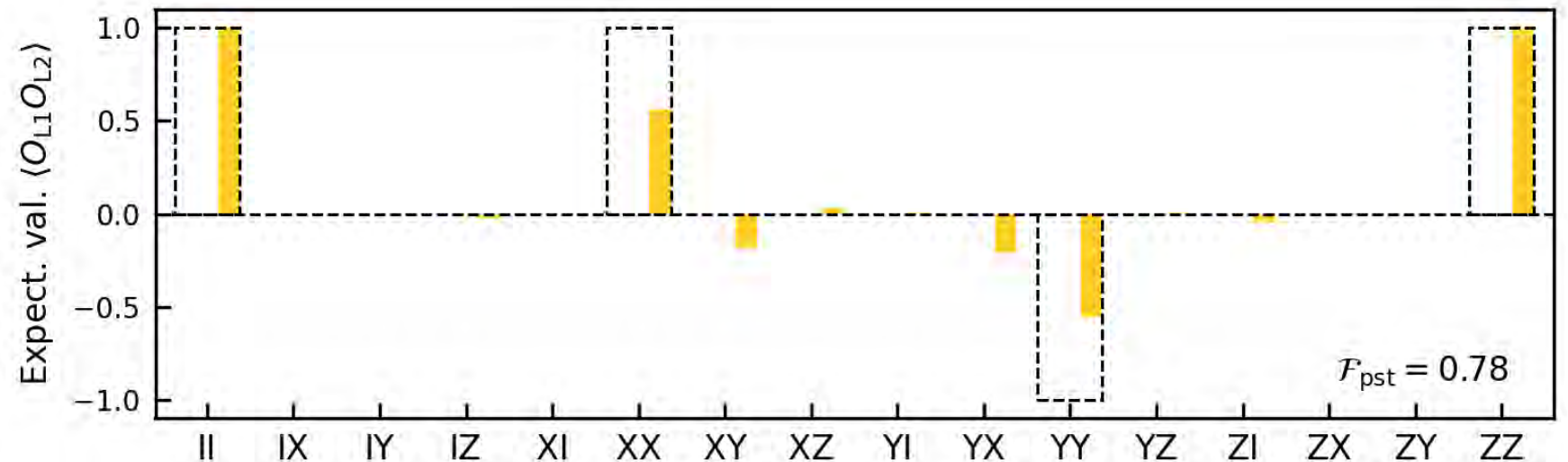


# Logical State Tomography

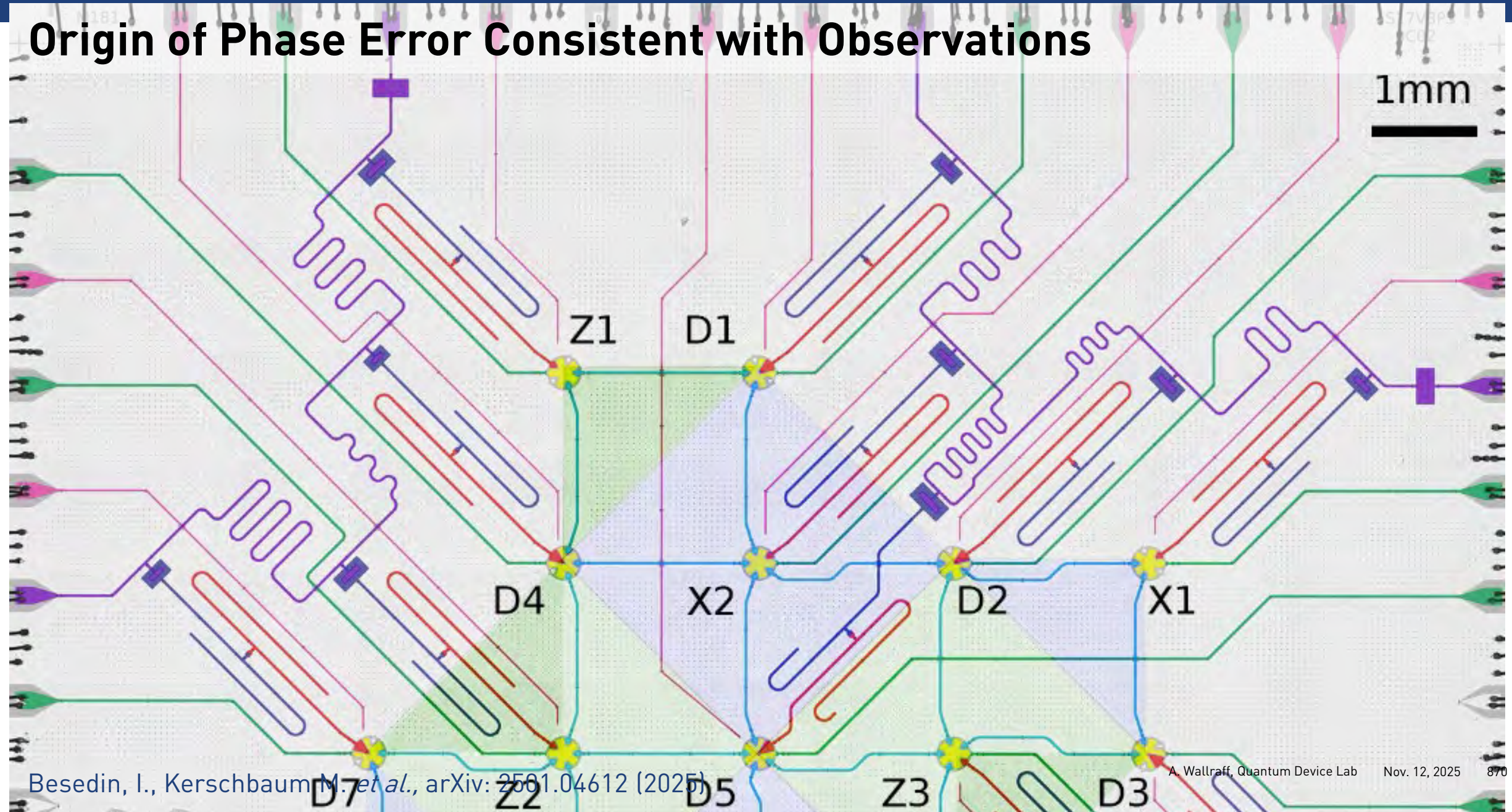
- Measure **all nine basis combinations of repetition code logical qubits** to perform **logical quantum state tomography**

## Note

- Non-zero  $X_{L1}Y_{L2}$  and  $Y_{L1}X_{L2}$  expectation values
- Consistent with a  $0.11\pi$  phase error on the first logical qubit state

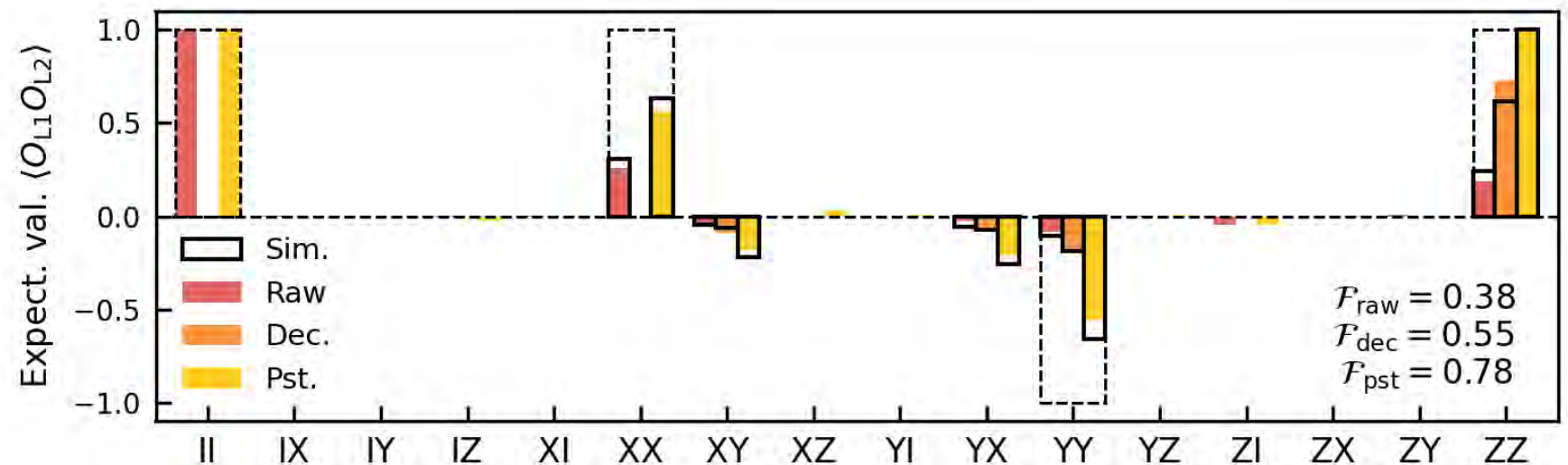


# Origin of Phase Error Consistent with Observations



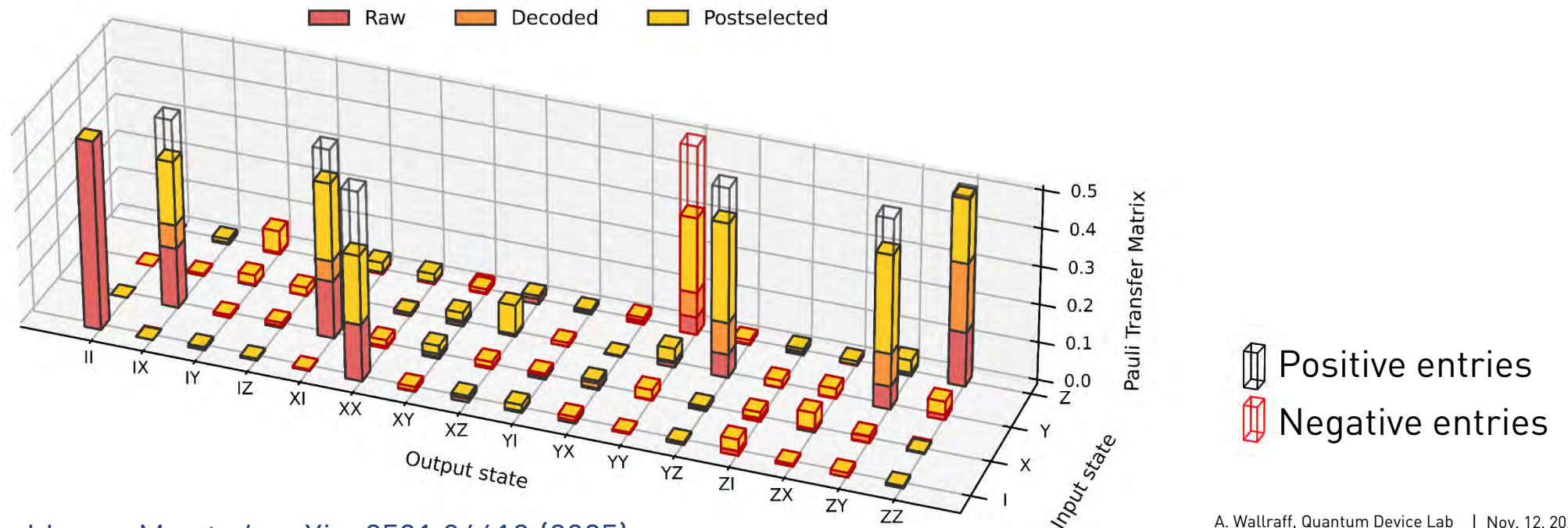
# Logical State Tomography

- Measure **in all nine combinations of bases of logical qubits** to perform **logical quantum state tomography**
- Use **MWPM decoder**:
  - raw  $Z_{L1} Z_{L2} = 0.19$  is improved to 0.73
- Good agreement of data with Pauli error model **simulations** based on randomized benchmarking (RB) and coherence measurements (+ coherent error on D1)



# Logical Quantum Process Tomography

- Split acting on logical input states  $|0\rangle_L, |1\rangle_L, |+\rangle_L, |-\rangle_L, |+i\rangle_L, |-i\rangle_L$  states
- Split operation maps Pauli operators to Pauli operators
- Note: single-qubit phase rotation of  $0.11\pi$  on logical qubit 1 corrected for.
- Pauli transfer matrix (PTM) representation
  - ideal values  $\pm 1/2$
- Process fidelity
  - raw:  $\mathcal{F} = 0.310(12)$
  - decoded:  $\mathcal{F} = 0.442(12)$
  - post-selected:  $\mathcal{F} = 0.80(3)$

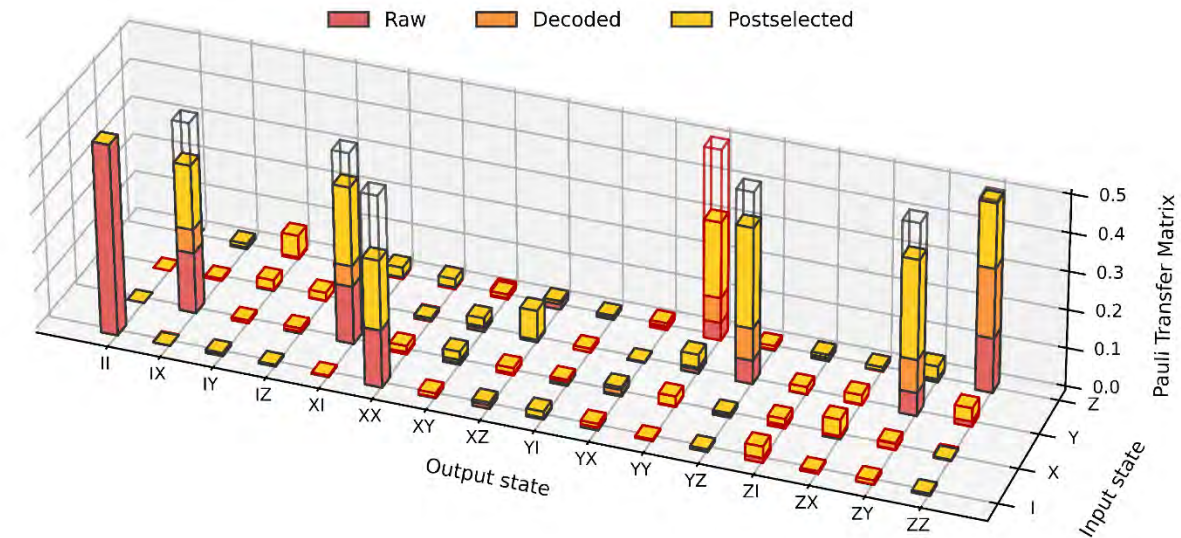
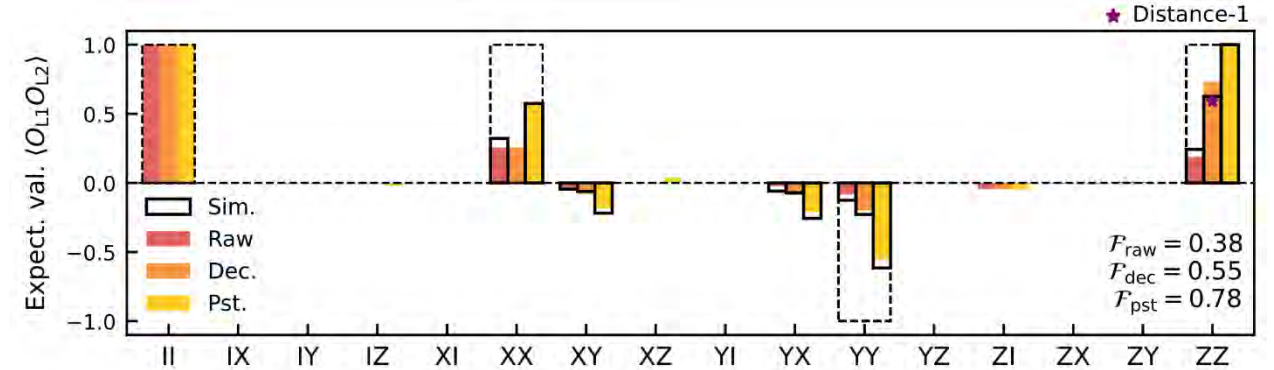


# Summary and Outlook

- Demonstrated **lattice surgery** on a distance-three surface code, **creating a logical Bell state** of two distance-three repetition codes
- **Increased decoded observable expectation value** compared to non-encoded variant
- Measured **logical Pauli-transfer matrix** for lattice split operation

## Outlook

- Deploy full scheme on two distance-three surface codes and integrate in **logical state teleportation protocol**



# The Quantum Device Lab



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